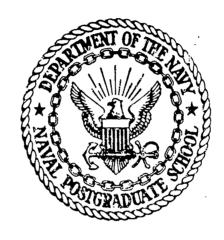
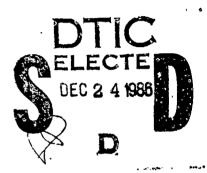
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NAVAL POSTGRADUATE SCHOOL

Monterey, California





THESIS

STRAIN DEPENDENT DAMPING CHARACTERISTICS
OF A HIGH DAMPING
MANGANESE-COPPER ALLOY

Dwight D. Dew

September 1986

Thesis Advisor:

Y. S. Shin

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Prepared for: David W. Taylor Naval Ship R & D Center Annapolis, MD 21402

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NAVAL POSTGRADUATE SCHOOL Monterey, CA 93943-5000

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	REPORT DOCUM	MENTATION	PAGE		
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2a. SECURITY CLASSIFICATION AUTHORITY		3 . DISTRIBUTION	/AVAILABILITY OF	REPOR	रा
2b. DECLASSIFICATION / DOWNGRADING SCHEDU	.E	Distribution unlimited.			
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6c. ADDRESS (City, State, and ZIP Code)		7b. ADDRESS (Cit	y, State, and ZIP Co	ode)	
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11 TITLE (Include Security Classification)					
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12 PERSONAL AUTHOR(S) LCDR DWIGHT D. DEW, USN					
13a TYPE OF REPORT 13b TIME CO Masters Thesis/Technical ROM 8 F	OVERED eb86 10 30 Sep8	14 DATE OF REPO	RT (Year, Month, De eptember	ay) 1	S PAGE COUNT 145
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The Naval Postgraduate School is investigating measurement techniques for the determination of strain-dependent damping characteristics of materials in an air environment. The material is a high damping manganese-copper alloy called sonoston. The measurement techniques employ cantilevered flat beam specimens in bending and cylindrical specimens in torsion. The specimens were subjected to three different heat and aging treatments. Pure random and sinusoidal sweep excitations are used as an excitation source in the frequency range of 20 to 500 Hz. Miniature accelerometers and strain gages were mounted on the specimens to obtain both input excitation and output responses. The results of the investigation are presented graphically as damping factor vs. resonant frequency, damping factor vs. strain, damping factor vs. input acceleration, strain vs. resonant frequency, strain vs. input acceleration, and input acceleration vs. resonant frequency.					
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Strain Dependent Damping Characteristics of a High Damping Manganese-Copper Alloy

by

Dwight D. Dew Lieutenant Commander, United States Navy B.A., University of South Florida, 1975

Submitted in partial fulfillment of the requirements for the degrees of

M.S. IN MECHANICAL ENGINEERING and MECHANICAL ENGINEER

from the

NAVAL POSTGRADUATE SCHOOL September 1986

Author:	Deroll & Su-	
	Dwight D. Dew	
Approved by:	Journg V. Then	
	Young'S. Shin, Thesis Advisor	
	Golf Pechins	
	faul Thuring for	
***************************************	Anthony Mealey, Chairman, Department of Mechanical Engineering	
	John N. Dyer,	
	/ John N. Dyer,	
	Dean of Science and Engineering	

ABSTRACT

This paper presents the studies on measurement techniques developed for the determination of strain-dependent damping characteristics of materials in an air environment. The material is a high damping manganese-copper alloy called Sonoston. The measurement techniques employ cantilevered flat beam specimens in bending and cylindrical specimens in torsion. The specimens were subjected to three different heat and aging treatments. Pure random and sinusoidal sweep excitations are used as an excitation source in the frequency range of 20 to 500 Hz. Miniature accelerometers and strain gages were mounted on the specimens to obtain both input excitation and output responses. The results of the investigation are presented graphically as damping factor vs. resonant frequency, damping factor vs. strain, damping factor vs. input acceleration, strain vs. resonant frequency, strain vs. input acceleration, and input acceleration vs. resonant frequency.



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ACKNOWLEDGEMENTS

I would like to express my appreciation to Professor Young S. Shin and Dr. Kil Soo Kim for their support and patience in making this project a productive task.

My appreciation is also expressed to Professor Jest Perkins who took the time to conscientiously review this work and to Mrs. Kathy Wong and Mr. Bob Hardy of the David W. Taylor Naval Ship R&D Center for their continued support of the work being done at the Naval Postgraduate School.

Additionally, I commend the conscientious efforts and the high quality of the support from the mechanical engineering shop facility at the Naval Postgraduate School, specifically, Mr. Charles Crow.

I. INTRODUCTION

A. GENERAL AND OBJECTIVE

Minimizing vibrations has long been an important part of engineering design. Suppressing noise and vibrations, especially in the lower frequency ranges, is very important for the Navy since submarines and surface ships become quieter and detection becomes more difficult. Noise suppression usually is accomplished by using high-damping non-metallic materials to isolate the machinery from the hull; or by dissipating the energy within the structure. The Navy's primary efforts have been on isolating the machinery. The methods of isolation include:

- 1. Use of a viscoclastic mount.
- 2. Blanketing the structure.
- 3. Increasing the stiffness of the structure creating the noise.
- 4. Tu .: r...
- 5. Reducing manufacturing tolerances.

Among these methods extensive use of resilient mounts is the primary approach used. This stems partly from the fact that hardly any structural metal or alloy possesses any significant damping capacity. If a metal or alloy with a high damping capacity could be found, ship silencing could be better accomplished by using these energy absorbing materials as component parts.

Damping is a property of a structure describing how rapidly vibration decays once it is excited. It is a function of many variables such as geometry, exciting frequency, temperature, and stress/strain level. Cast iron has been considered to be the only acceptable structural material with significant damping capacity currently available. However, it can be seen (Figure 1.1) that other materials are also available, especially the manganese-copper alloys.

The objective of this thesis is to recommend a standardized measurement technique to provide consistent and reliable damping characteristics of high damping alloys.

B. BACKGROUND

Initial Naval Postgraduate School material damping research implemented a testing procedure for measuring viscous damping in large metal plate specimens at low

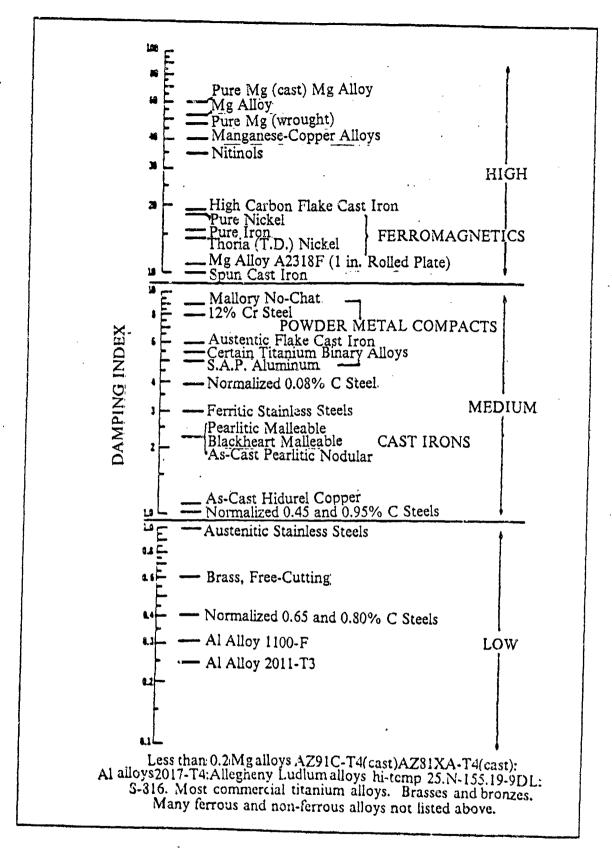


Figure 1.1 Material Damping Index (Ref. 1)

stress levels using an impulse hammer technique. The specimen could be placed in an environmental chamber for testing in either an air or water environment. Temperature control allowed testing to be conducted in the range of 30°F, to 90°F [Ref. 2]. Further testing introduced and validated a random force excitation technique adapted for underwater use and examined the effects of four specimen boundary conditions on system damping measurements [Ref. 3]. Following this work the environmental chamber was utilized to investigate how the damping characteristics of a cast nickel aluminum bronze plate specimen varied in both an air and a saltwater environment. Work to determine the damping characteristics of composite and constrained layer plates was also performed [Ref. 4].

This paper presents an investigation to determine how the damping characteristics of a high damping manganese-copper alloy vary with strain in an air environment.

C. MIN-CU ALLOYS

The high damping capacity of Mn-Cu alloys gives it great potential as a structural metal.

Previously the alloys were found physically unsatisfactory because of poer quality castings. More advanced alloys tested later were found physically sound but susceptible to general corrosion and stress cracking. [Ref. 1:p. 15]

Their susceptibility to corrosion and stress cracking made them unsatisfactory for marine use.

In general, alloys that possess high damping capacity are not usually the best adapted to construction purposes since the gain in damping is often at the expense of stiffness, strength, durability, corrosion resistance, cost, machinability, or long-term stability. [Ref. 5:p. 64]

Situations (especially in the Navy' where these high damping materials can be utilized do occur. A commercially produced Mn-Cu alloy (Sonoston), with a composition of 54.25 wt% Mn, 37.0 wt% Cu, 4.25 wt% Al, 3.0 wt% Fe, and 1.5 wt% Ni, could be used in gear trains, brake discs. etc. (Figure 1.2).

Potential applications of quiet metals

General:

Plug inserts to noisy machine parts

Cladding for virtually any noisy part

Reduction of resonant amplification factors

Attenuation of ringing

Machinery diagnostic techniques

Specific:

Gears and gear webs

Pump castings

Diesel engine parts

Brake discs

Wheel rims

Supmarine/torpedo/ship propellers

Helicopter gears

Hachinery frames and bases

Aircraft/missile structural members

Phonograph pickups/playing arms

Transducers

Office/textile/printing machinery components

Hi-fi audio micropnone components

Bimetallic strips-control devices

Plates for tuning capacitors

Resistors

Hearing aid components

Movie camera gears, etc. etc.

Figure 1.2 Potential Applications (Ref. 6)

D. METALLURGY OF MN-CU ALLOYS

The fact that Mn-Cu Alloys can have a high damping capacity has been known for years. High damping is associated with alloys greater than 20% Mn with practical alloys ranging from 70%Cu-30%Mn to 30%Cu-70%Mn. To properly condition these alloys to obtain high damping capacity, four heat-treatment steps are required: (Figure 1.3)

- 1. Solution treatment in (yMn) single phase region (a face centered cubic structure).
- 2. Water quenching to retain the single phase metastable supersaturated solid structure.
- 3. Aging treatment in the two phase $(\gamma Mn + \alpha Mn)$ region.
- 4. Water quenching to room temperature (a martensitic type transformation of the matrix occurs during this time). (Figure 1.4)

The structure of the quenched solution treated sample is face centered cubic (FCC), but becomes tetragonal if aged between 400°C - 600°C . Aging produces areas of manganese enrichment prior to the precipitation of α -Manganese where the tetragonal structure can exist at room temperature. On cooling from the aging temperature, the transformation, nucleated at dislocations and α -precipitate, occurs by a diffusionless shear process (martensitic). The tetragonal phase has the same volume as the cubic structure from which it is formed; and to minimize internal strains, the matrix becomes self-accomodating by splitting up into domains of common orientation analogous to martensitic platelets or mechanical twins. [Ref. 7:p. 4]

When the material is stressed, deformation occurs by movement of the domain boundaries, resulting in a macromechanical hysteresis effect. This is a reversible process causing no damage. This strain induced reorientation of the tetragonal domains causes the high damping capacity. Damping capacity increases with aging time up to 8 hours as the number of microtwins increases. After aging for 9 hours the density of microtwins gradually decreases until after 20 hours they can only occasionally be seen. Therefore, the optimal aging time is 8 hours in order to get the highest damping capacity.

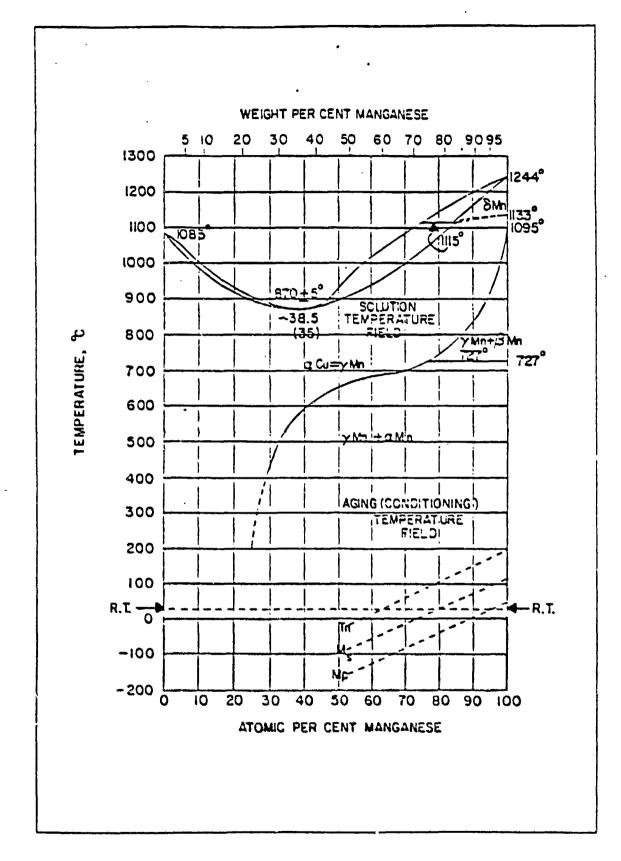


Figure 1.3 Cu-Mn Binary Phase Diagram (Ref. 1)

```
Summary of nest Treatment Effects in Cu-Mn Alloys
Step 1: Solution treatment:
                        * ($4 ) (A1:FCC)
Step 2: Quench from solution treatment temperature:
               If < 80 m/o Pm: v recained 9 North temperature
               If > 80 w/o Hm: +
                        antiferromagnetic ordering. # T
                        martensitic transformation \theta = (T_{\mu} \Rightarrow H_{\mu})
Step 3: Aging treatment (assuming alloy < 80 w/o Nm) (in two-dnase region:
                                + (Al:FCC) + e (Al2: complex SCC))
           Stage I: - (initial) (Mn-enriched) (matrix) - " (metastable
                                                             Cu-rich precipitates, 100A)
                                          (Mn-enriched (matrix) + " + a
           Stage Il:
                                                             (Wiomenstatten precipitate)
                                              dissolves (madesieted) + / dissolves (madesieted) + / dissolves
           NOTE: The condition of Stage II is typically that leading to
           nois: The condition of Stage II is typically that leading to continue despine; Stage III is oversaces, i.a. no martensitic transformation of the The Matrix will occur on subsequent quenching - such will occur only if the matrix is conditioned to the necessary **Marrich State by metastable ***
           precipitation.
Step 4: Guener from the sound treatment (assuming Stade 11 condition from
                                                                 Step 3 apove ;:
           - (Mn-enriched) -
                                                                  (Jauons Ifame) ....
              entiferromagnetic
              orcering & ig
              martensitic trans-
                                                  retained ?
                                                                          retained
              formation # Mg
              NOTE: The martensitic transformation is trigogred
                       by the itrain associated with the tetragonal distortion (FCC - FCT)of the antiferromagnetic
                       ordering reaction; TH . H.
```

Figure 1.4 Summary of Heat Treatment (Ref. 1)

Mn-Cu alloys have several unique problems because of their metallurgy. Their strength and hardness increases during the aging process while their damping capacity decreases with increasing temperature. The damping capacity is reduced drastically at the transformation temperature (100°C to 200°C) where the material returns to a cubic structure. Since the cubic-tetragonal transformation is well below room temperature, storage at room temperature is equivalent to a low temperature aging leading to a decrease in damping capacity over a few years.

II. CANTILEVER BEAM EXPERIMENTAL METHOD

A. GENERAL

Two measurement techniques were developed for the determination of strain-dependent damping characteristics of Sonoston in an air environment. The measurement techniques employ cantilevered flat beam specimens in bending and cylindrical specimens in torsion. The specimens were subjected to three different heat and aging treatments. Pure random and sinusoidal sweep excitations are used as an excitation source in the frequency range of 20 to 500 Hz. Both methods use transfer function techniques. Miniature accelerometers and strain gages were mounted on the specimens to obtain both input excitation and output responses.

B. METHOD

Sonoston is a non-linear metal with a nominal Modulus of Elasticity (E) of 12 x 10⁶ psi and a yield strength of 45 Kpsi. Since aging increases the Modulus of Elasticity, it was decided that 3 tensile specimens would be tested. All three specimens were solution annealed at 800°C for 45 minutes. One was aged for 1 hour at 425°C, one was aged at 425°C for 2 hours, and the third was left unaged. Engineering Stress/Strain curves were constructed from the test results (Figure 2.1). The Young's Modulus used in further calculations was obtained from these results. For the unaged sample E was calculated as 17.5 x 10⁶ psi; for the 1 hour aged sample E was 19.7 x 10⁶ psi; and for the 2 hour aged sample E was 25.5 x 10⁶ psi. These values were then used to calculate the resonant frequencies of the cantilever beam specimens as well as that of the torsion samples (Appendix B).

Five cantilever beam specimens were then manufactured and solution annealed. Two specimens were aged for 1 hour, two were aged for 2 hours, while the fifth was left unaged. Three strain gages were mounted on each specimen at locations where the maximum strain due to bending moment occurs. With L the total length of the cantilever beam from the root to the tip and X being the distance along the beam measured from the root, Reference 8 lists the locations where maximum bending occurs for the first three modes in X/L increments of 0.04. A Fortran program was written to calculate the moment for any point along the beam in X/L increments of 0.01 (Figure 2.2).

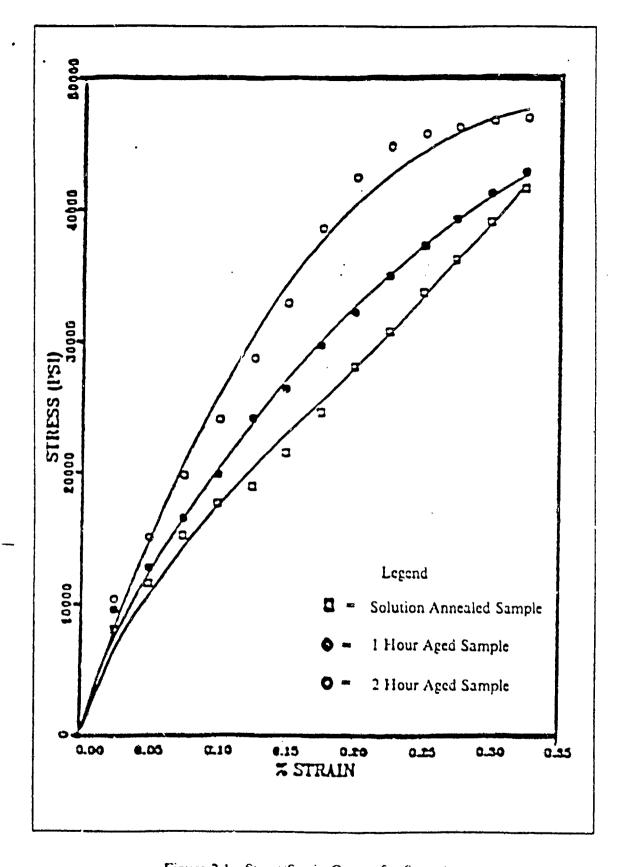


Figure 2.1 Stress/Strain Curves for Sonoston

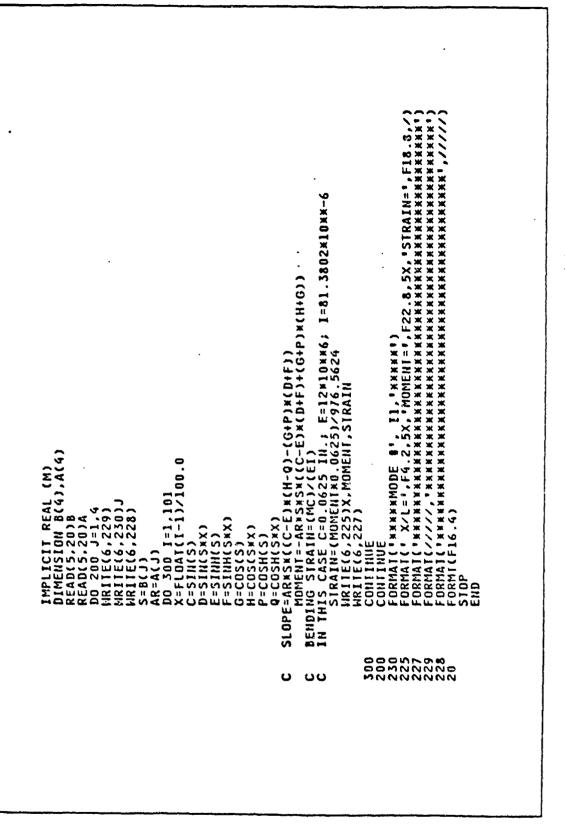


Figure 2.2 Fortran Program for Location of Maximum Strain

For mode 1 the maximum moment occurs at the root; for mode 2 it occurs at the root and at X/L=0.53; for mode 3 it occurs at the root, X/L=0.31, and at X/L=0.71. In all three modes the maximum moment occurs at the root of the beam and for mode 3 the moment at X/L=0.71 was greater than at X/L=0.31. Based on this information the three strain gages were mounted on all the cantilever beams at a) the root, b) at X/L=0.53, and c) at X/L=0.71 (Figure 2.3).

The beam samples were then placed in the test fixture for testing (Figure 2.4). By monitoring the acceleration of both the supporting system and the beam tip, the response frequency can be determined. Two 4-mg Endevco 2250A-10 accelerometers were mounted, one on the supporting structure above the root of the cantilever beam and the other on the tip of the beam (Figure 2.5). A random input signal was generated by the HP 3582 spectrum analyzer and was then passed through the Crown solid state amplifier to the electromechanical vibration generator (Figure 2.6). The accelerometer output was passed through a Endevco 4416A Signal Conditioner to the HP 5451-C Fourier Analyzer for processing.

To get an initial idea where the specimen's natural resonant frequencies lie in the frequency spectrum, a baseband measurement was made from 0 to 1KHz. These measurements for the solution treated sample, 1 hour aged sample, and 2 hour aged sample are shown in Figures 2.7 to 2.9. Use of Band Selectable Fourier Analysis (BSFA or zoom) was then used on the first three resonant frequencies.

The RMS input acceleration level (root accelerometer) was determined as follows: A signal in the time domain was captured for a 5mSec period (Figure 2.10), squared and then integrated for the period. The square root was then calculated and multiplied by the conversion factor to obtain mv. Ten time samples were taken for an average value. This value was then converted to g by dividing by a calibration factor (10.31 mv/g) which was determined as described in section C of this chapter. This gives the RMS g level. The RMS strain level was determined in the same way. In this case the strain signal was sent through an Ectron (model \$63F) strain gage amplifier calibrated so that 2.5V dc = 10,000µstrain. (Figure 2.11)

Swept sine tests were performed using the HP-3562A Signal Analyzer. Measurements of input acceleration and strain were made in the same way except that, since the strain and input force varies with frequency, the time domain data was obtained at the peak of the transfer function.

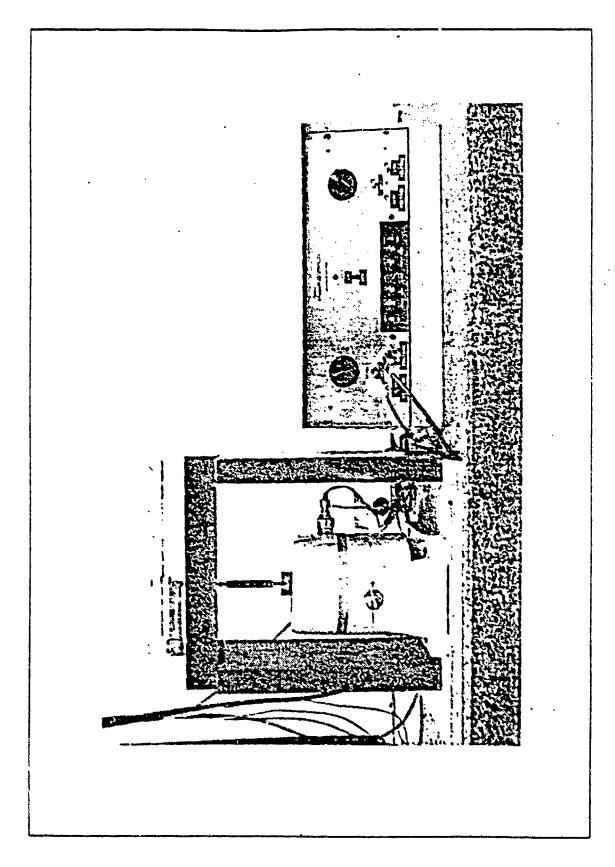


Figure 2.4 Cantilever Beam Test Fixture

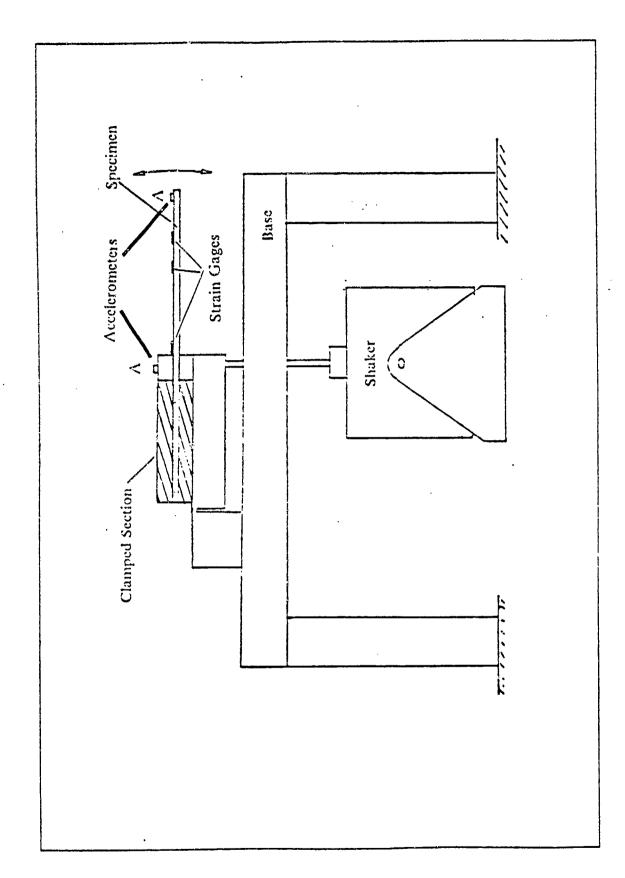


Figure 2.5 Accelerometer Location

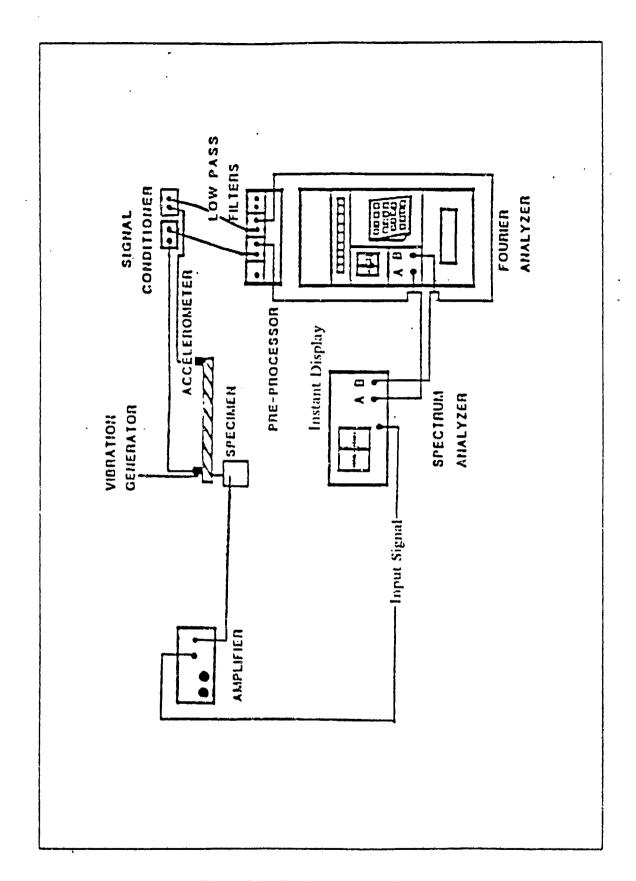


Figure 2.6 Equipment Line Diagram

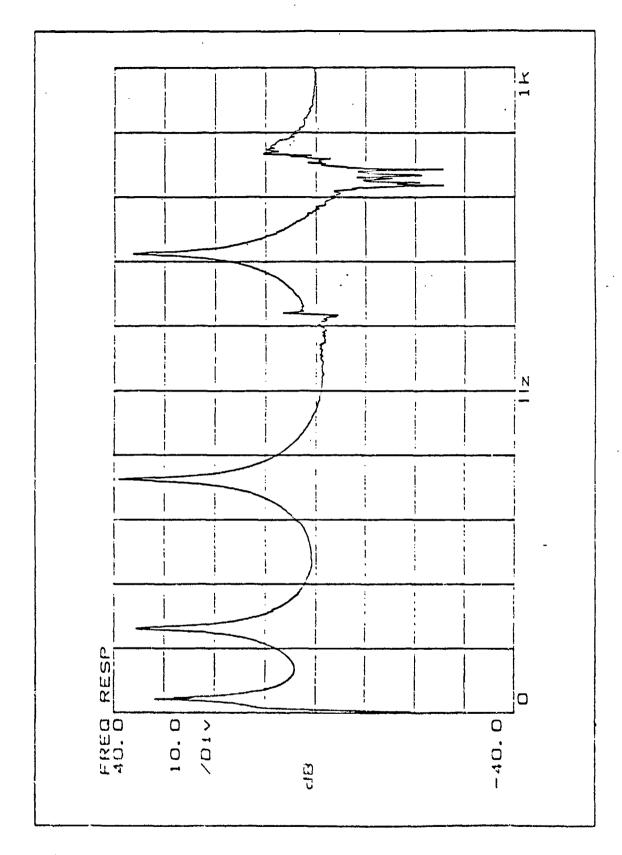


Figure 2.7 Baseband Measurement of the Solution Annealed Sample

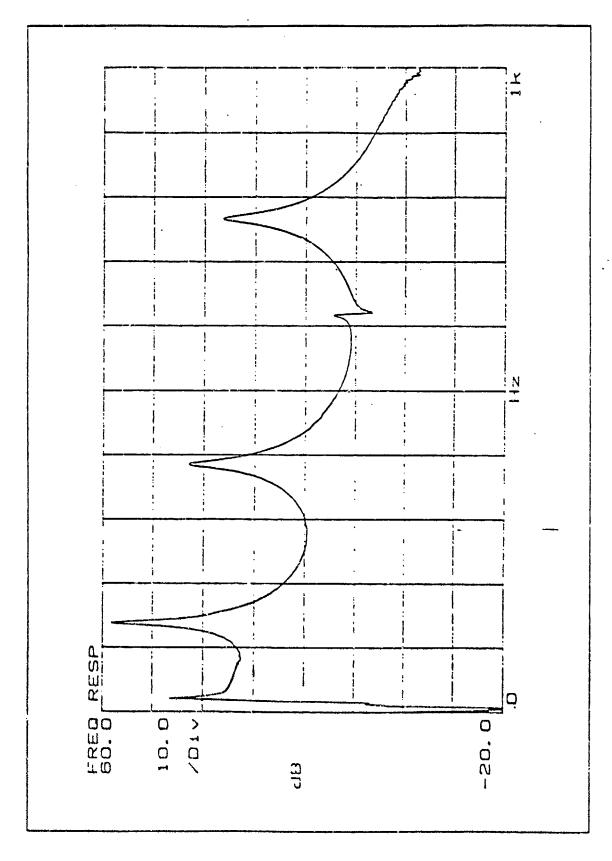


Figure 2.8 Baseband Measurement of the 1-Hour Aged Sample

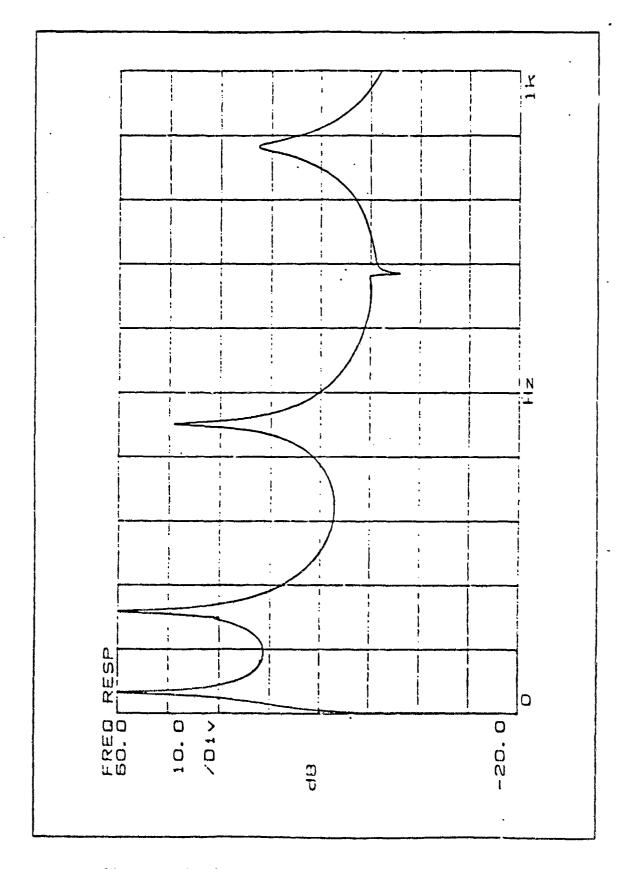


Figure 2.9 Baseband Measurement of the 2-Hour Aged Sample

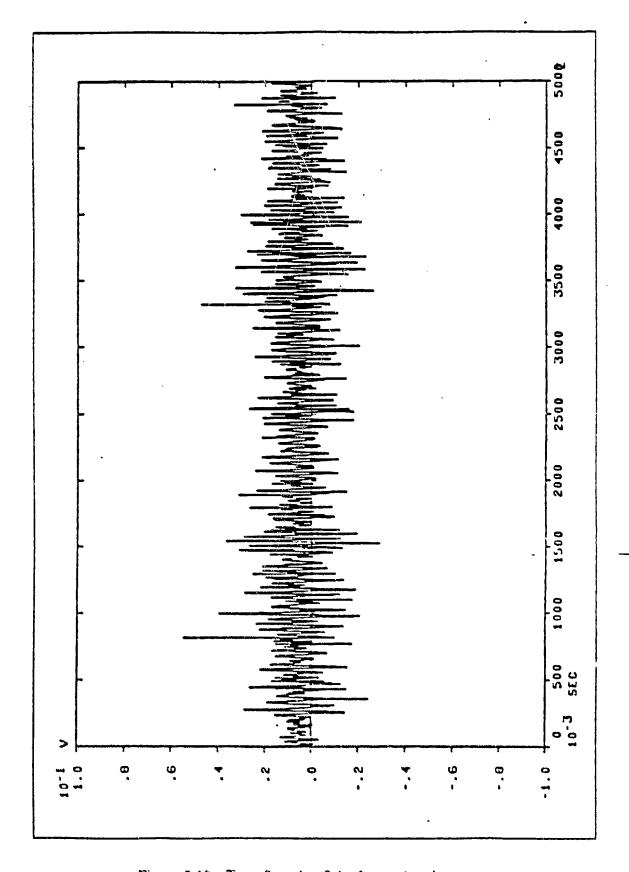


Figure 2.10 Time Sample of the Input Accelerometer

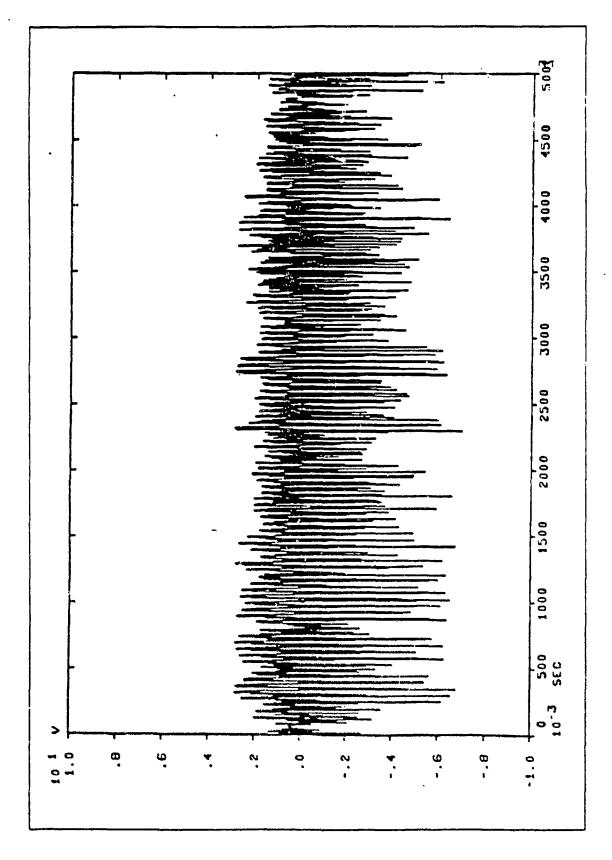


Figure 2.11 Time Sample of the Root Strain Gage

During the random input tests the output accelerometer was removed and the root strain gage was used as the output device in order to test the effect of mass loading of the beam by the 4 mg accelerometer. The resulting transfer function corresponded to that obtained by using two accelerometers. Both had the same resonant frequency and very similar loss factors but different function amplitudes (Figures 2.12 and 2.13). Since there is no mass loading effect due to the accelerometer at the tip of the beam, transfer functions could be obtained using either two accelerometers or one accelerometer and the strain gage.

Each mode was analyzed at six different amplification levels with two transfer functions being obtained at each level. Random noise tests were analyzed first followed by swept sine tests.

C. CALIBRATION

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The accelerometers used in the experiment were calibrated by a drop test (free-fall) to obtain the value of mv/g associated with each accelerometer. The HP-3562A Signal Analyzer was used to record the time signal trigger delay. Figures 2.14 and 2.15 show the results of one calibration run. Figure 2.15 is a blown up portion of Figure 2.14 showing just the free-fall voltage difference due to gravity. The voltage difference between the initial state and the first peak corresponds to 1g acceleration.

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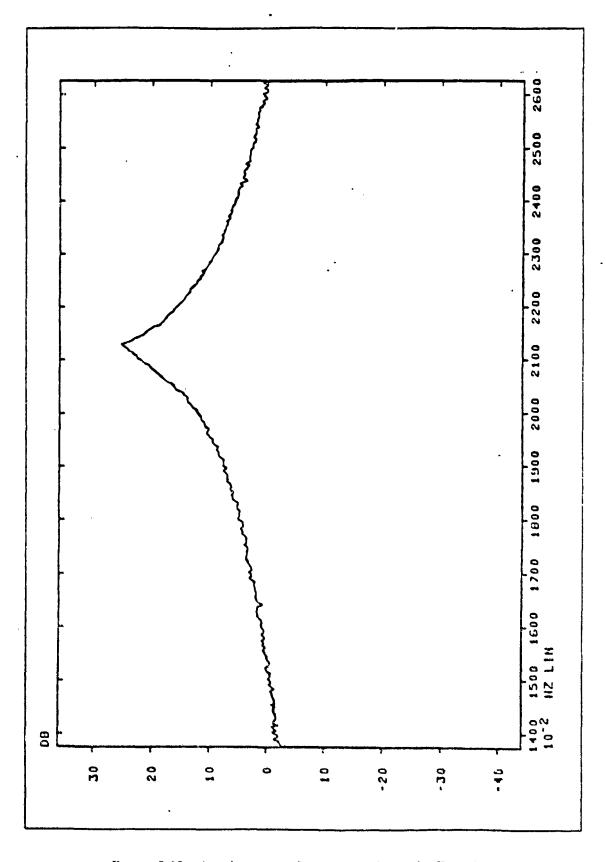


Figure 2.13 Accelerometer/Strain Gage Transfer Function

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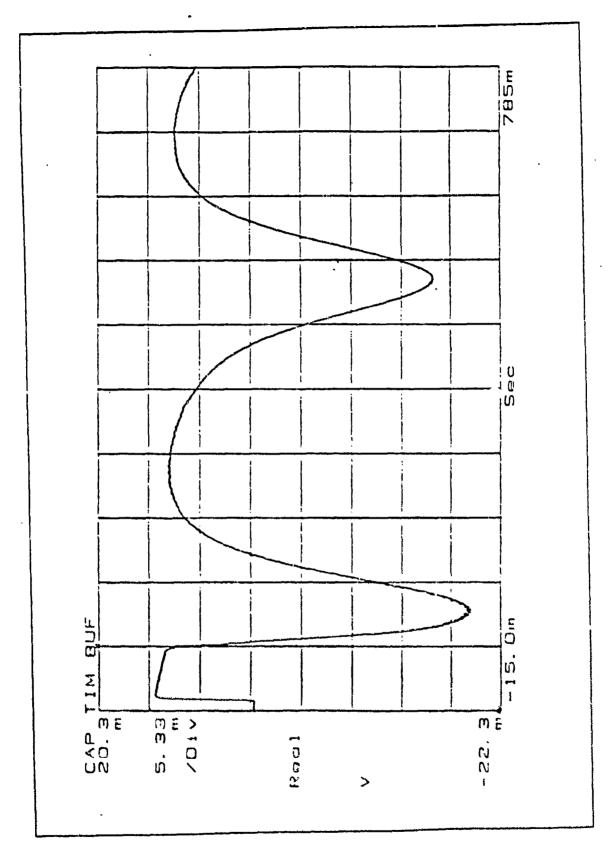


Figure 2.14 Calibration Curve

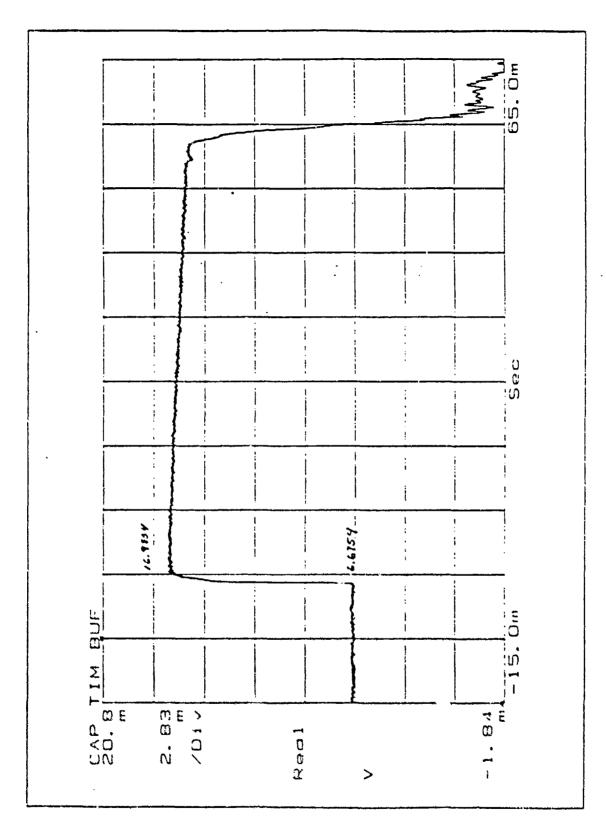


Figure 2.15 Free-fall Section

III. CANTILEVER BEAM RESULTS AND DISCUSSION

A. GENERAL

The cantilever beam samples give results in the frequency ranges 20-25 Hz (Mode 1); 130-160 Hz (Mode 2); and 360-445 Hz (Mode 3). Appendix D (part 1) shows a representative transfer function, in both log magnitude and linear scales, that was obtained after 32 time averages using a random input excitation source. A graph of the associated 180° phase shift, characteristic of a two complex pole system, is also in the appendix. The phase shift can give an indication of the loss factor when compared to other phase shift graphs since a gradual slope is indicative of a high loss factor. The coherence function, which is a measurement of the noise contamination and/or nonlinearity in the transfer function indicates how much of the system output is caused by the system input. A representative graph of the coherence function is also included in Appendix D. The dip in the coherence at the resonant frequency is due to the impedance mismatch between the output and input signals. The collected data from the random input and swept sine tests are listed in part 1 of Appendix E. These tables list the resonant frequency, computed loss factor, average strain, and average input acceleration.

B. INPUT ACCELERATION -VS- STRAIN

Figure 3.1 shows the Input Acceleration -vs- RMS Strain for Mode 1 using a random input. This RMS Strain value is determined from the average of ten 5mSec time samples taken from the root strain gage. The input acceleration value is determined in the same manner. Each sample was tested at six different amplification levels and shows that the strain increases with an increase in input acceleration in a linear fashion. It appears that the unaged and 1 hour aged samples follow the same trend while the strain for the 2 hour aged sample increases faster for smaller increases in input acceleration. Figure 3.2 is a graph of Input Acceleration -vs- Strain using a swept sine excitation source. The swept sine test was performed using the HP-3562 Signal Analyzer. The HP-3562 was set for 8 averages and a resolution of 400 points per sweep. The strain value in this case is obtained at the resonant frequency as is the input acceleration. In both tests, random and swept sine, the strain increases with input acceleration as expected. Figures 3.3 to 3.6 are graphs of Input Acceleration -vs-Strain for modes 2 and 3. In both mode 2 and mode 3 the strain increases as the input

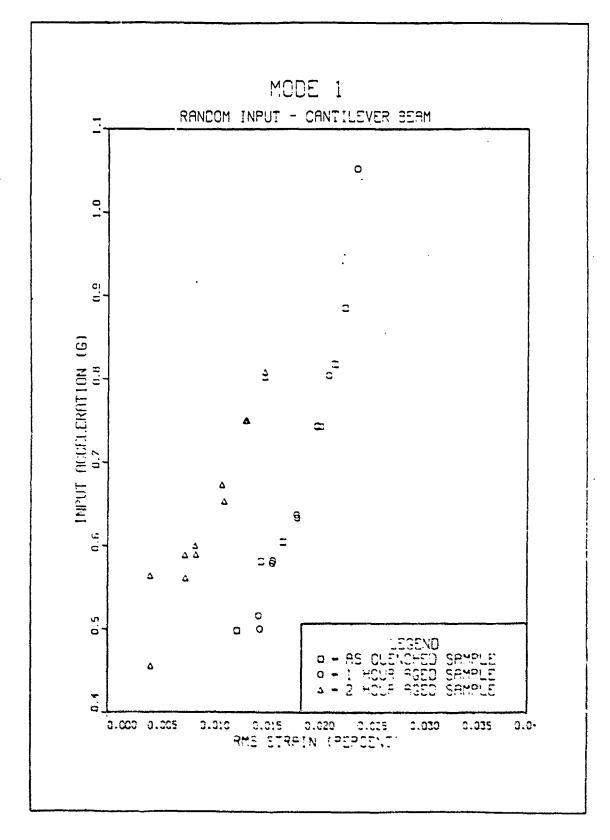


Figure 3.1 Mode 1 - Input Acceleration -vs- Strain (Random Input)

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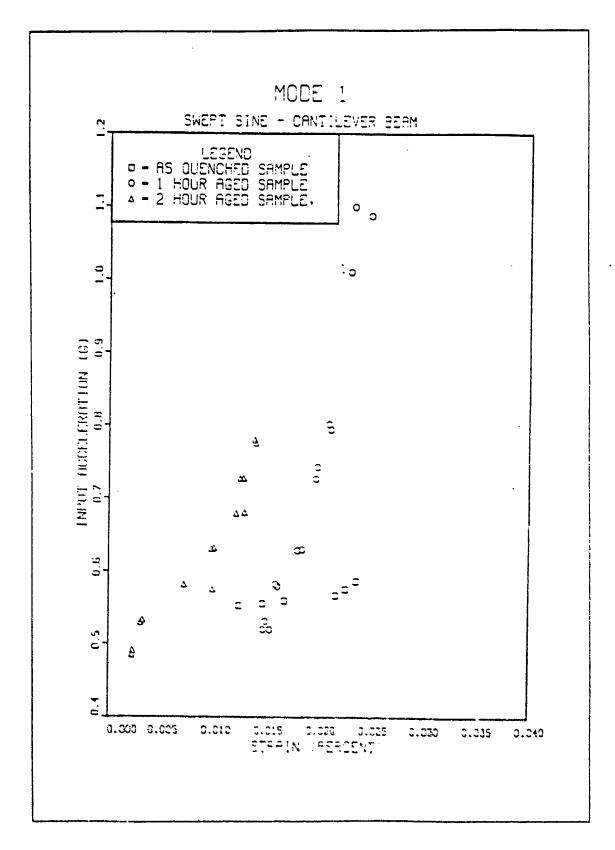


Figure 3.2 Mode 1 - Input Acceleration -vs- Strain (Swept Sine)

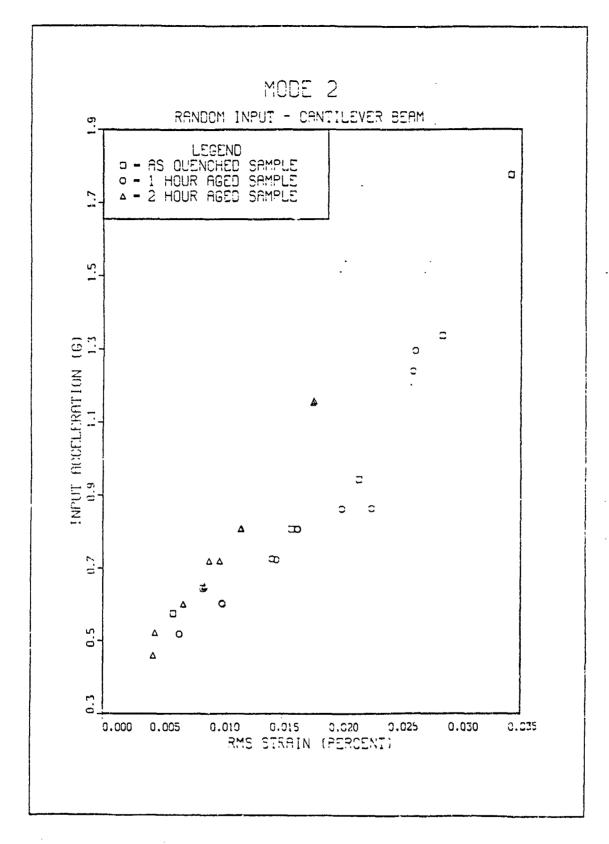


Figure 3.3 Mode 2 - Input Acceleration -vs- Strain (Random Input)

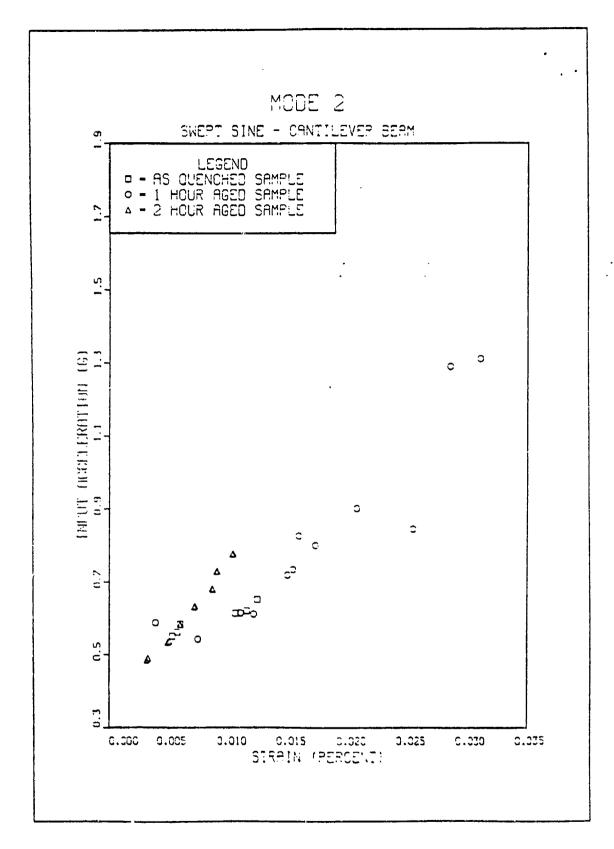


Figure 3.4 Mode 2 - Input Acceleration -vs- Strain (Swept Sine)

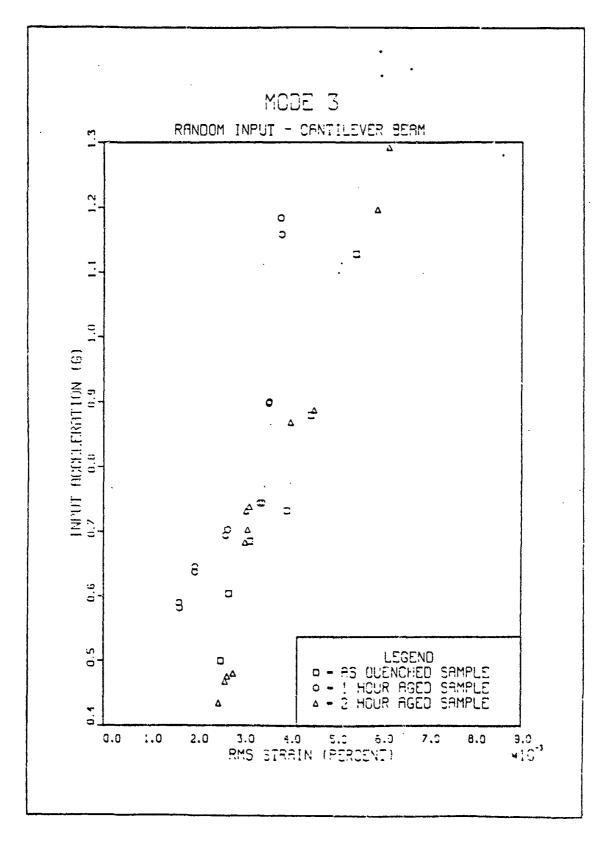


Figure 3.5 Mode 3 - Input Acceleration -vs- Strain (Random Input)

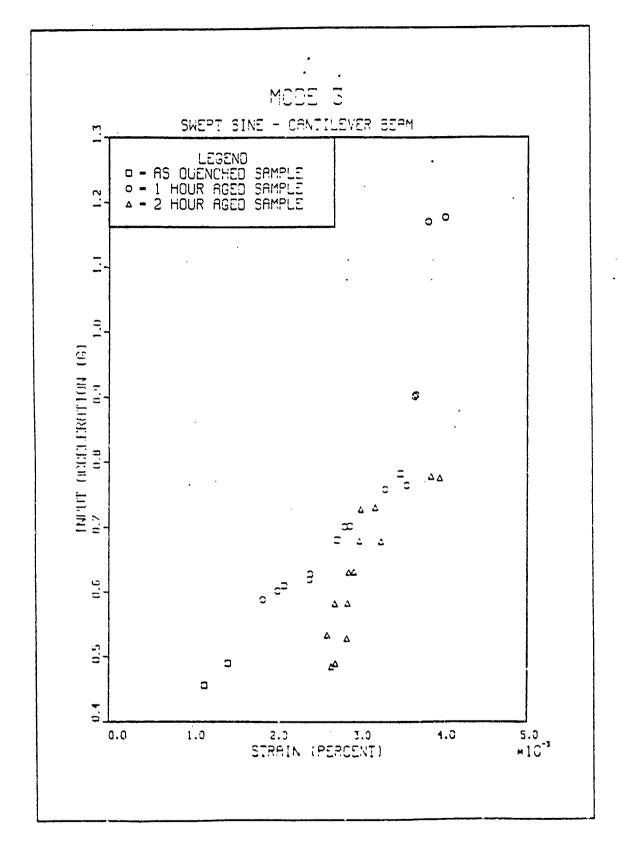


Figure 3.6 Mode 3 - Input Acceleration -vs- Strain (Swept Sine)

acceleration increases and seems to be consistent between the random tests and the swept sine tests. The root strain gage was used for all measurements as it gave the highest value of strain for all three modes.

C. LOSS FACTOR -VS- STRAIN

Figure 3.7 is a graph of Loss Factor -vs- RMS Strain for mode 1 random input. As the strain increases the loss factor increases. The aging time also plays a factor in the loss factor. As the aging time increases the loss factor increases. It appears that the loss factor of the 2 hour aged sample increases significantly at the 0.015% strain level. This could be due to the non-linearities in the material. Figure 3.8 is the mode 1 swept sine results of Loss Factor -vs- Strain. The results are very similar to those from random input tests. Both excitation sources give quite consistant results for tests repeated under similar conditions. Figures 3.9 and 3.10 are the mode 2 results. The trends seen in mode 1 are repeated here in mode 2 except that the loss factor has a lower value for all of the mode 2 samples. Figures 3.11 and 3.12 are the mode 3 results. As in modes 1 and 2, the loss factor increases with both increasing strain and increased aging time. The damping of mode 3 seems to be comparable with that of mode 2 but both are less than that found in mode 1. From looking at the baseband curves for each of the three heat treatments (Chapter 2), it would appear that the highest damping occurs in the second mode. However, actually measuring the loss factor shows that the first mode is the mode of highest energy dissipation. In all three modes, the random input and swept sine input tests give similar results. For all of the tests the geometry of the sample plays an important part in determining the level of bending strain and its associated loss factor. In order to compare the physical properties of different materials the geometry of the test samples must be the same.

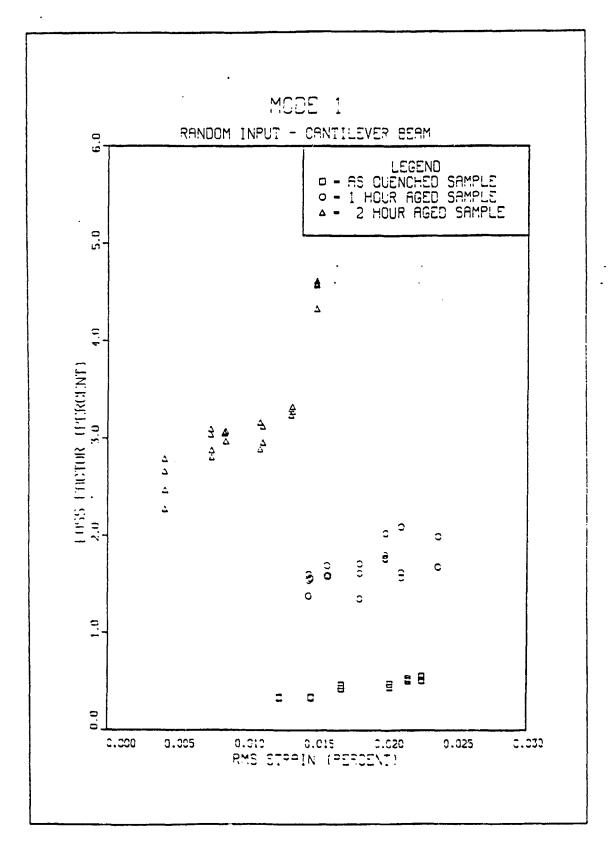


Figure 3.7 Mode 1 - Loss Factor -vs- Strain (Random Input)

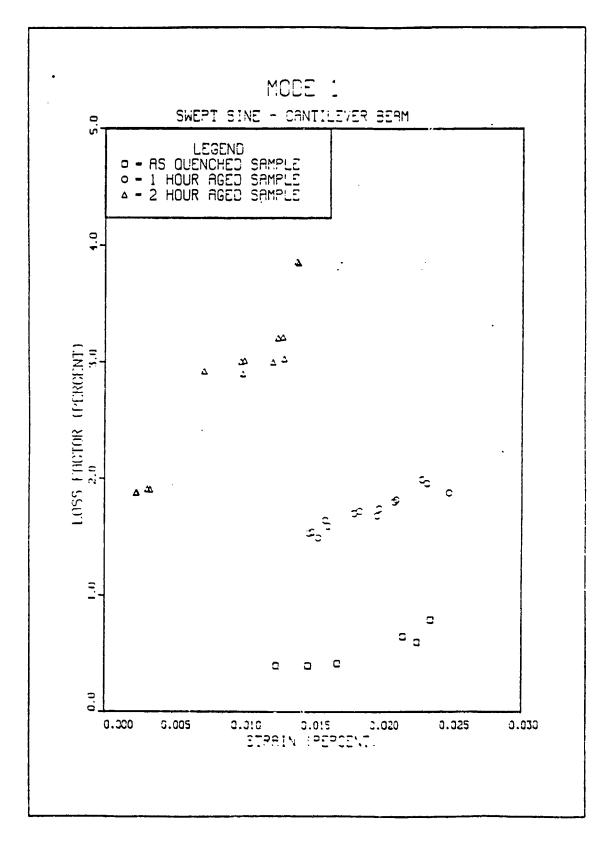


Figure 3.8 Mode 1 - Loss Factor -vs- Strain (Swept Sine)

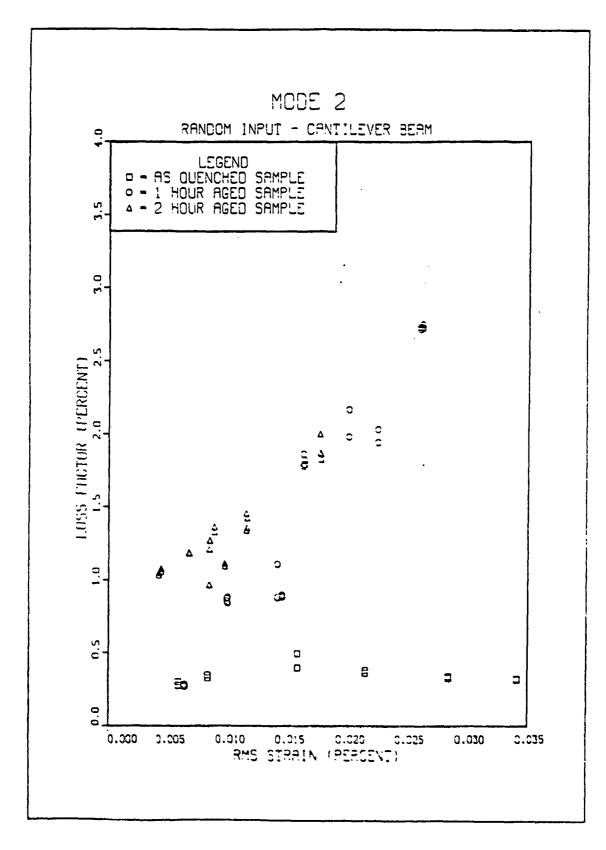


Figure 3.9 Mode 2 - Loss Factor -vs- Strain (Random Input)

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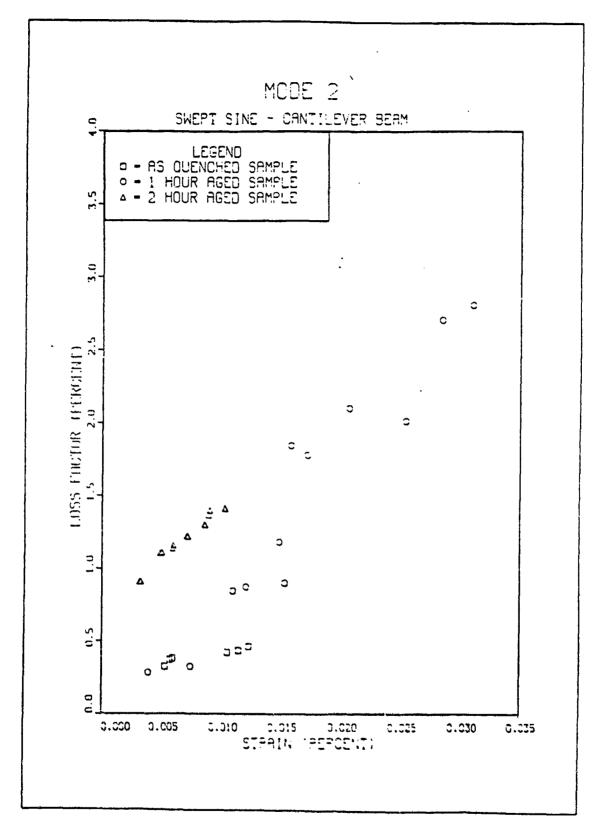


Figure 3.10 Mode 2 - Loss Factor -vs- Strain (Swept Sine)

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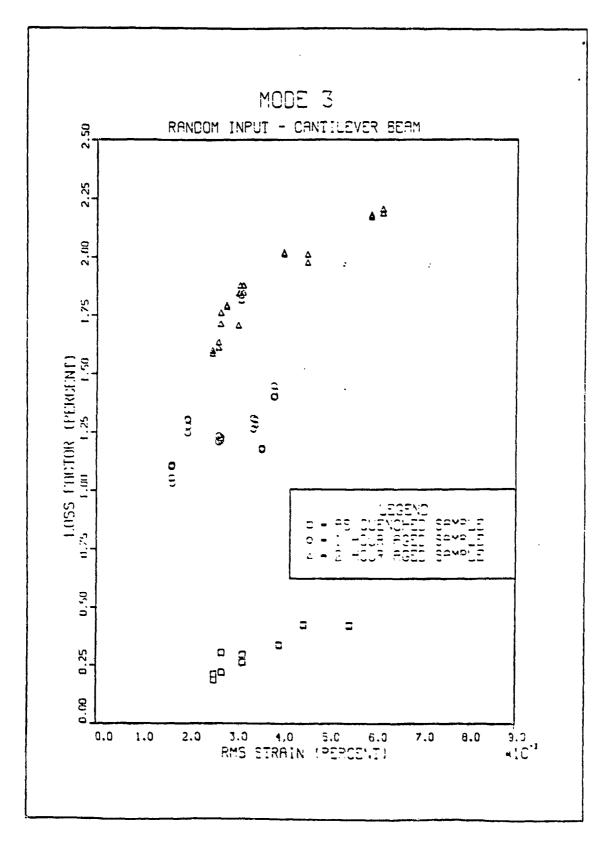


Figure 3.11 Mode 3 - Loss Factor -vs- Strain (Random Input)

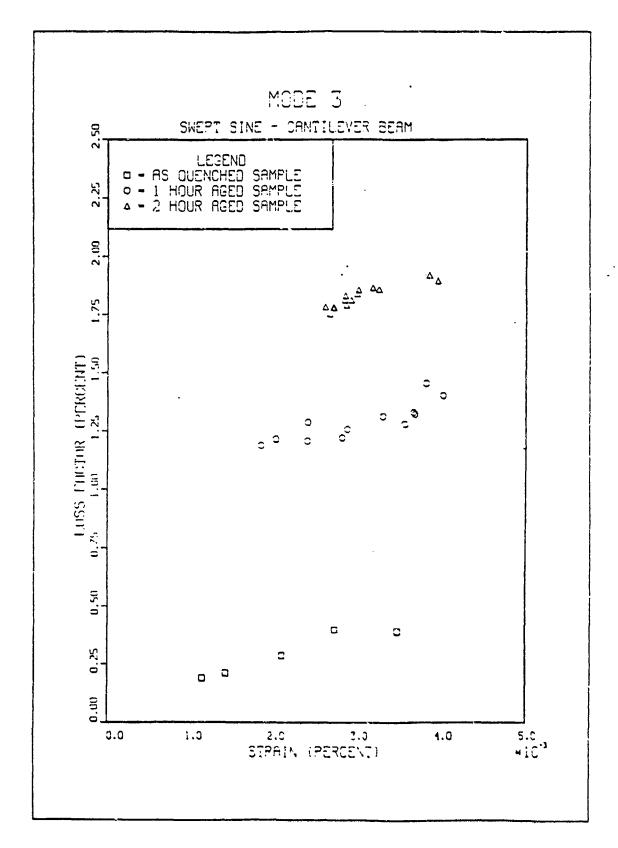


Figure 3.12 Mode 3 - Loss Factor -vs- Strain (Swept Sine)

D. STRAIN -VS- FREQUENCY

Figure 3.13 is a graph of the RMS Strain -vs- Frequency for mode 1 random input. For all of the samples as the strain increases the resonant frequency shifts downward. This increase in strain corresponds to a decrease in the Young's Modulus (see stress/strain curve in Chapter 2). Since Young's Modulus is needed in calculating the resonant frequency a decrease in E will result in a decrease in resonant frequency (Appendix B). As the aging time increases the downward shift in the resonant frequency becomes more pronounced as the strain increases. Figure 3.14 is the mode 1 swept sine results. Again, the results are comparable with those obtained from the random input tests. Figures 3.15 and 3.16 are the Strain -vs- Frequency results for mode 2. In both figures the 1 hour aged samples show the greatest frequency shift. The results between the two graphs are comparable. Mode 3 results are shown in Figures 3.17 and 3.18. The same downward shift of the resonant frequency as the strain increases appears here as in the other two modes.

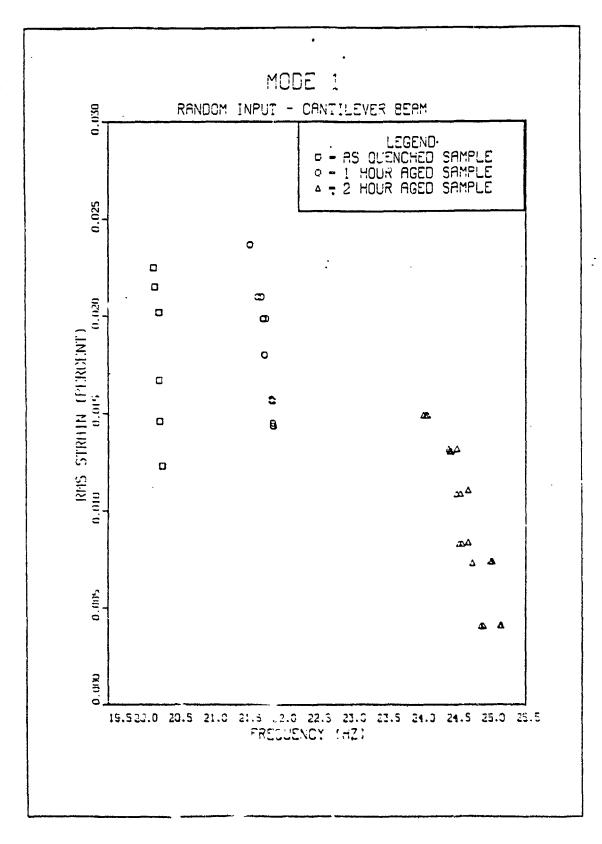


Figure 3.13 Mode 1 - Strain -vs- Frequency (Random Input)

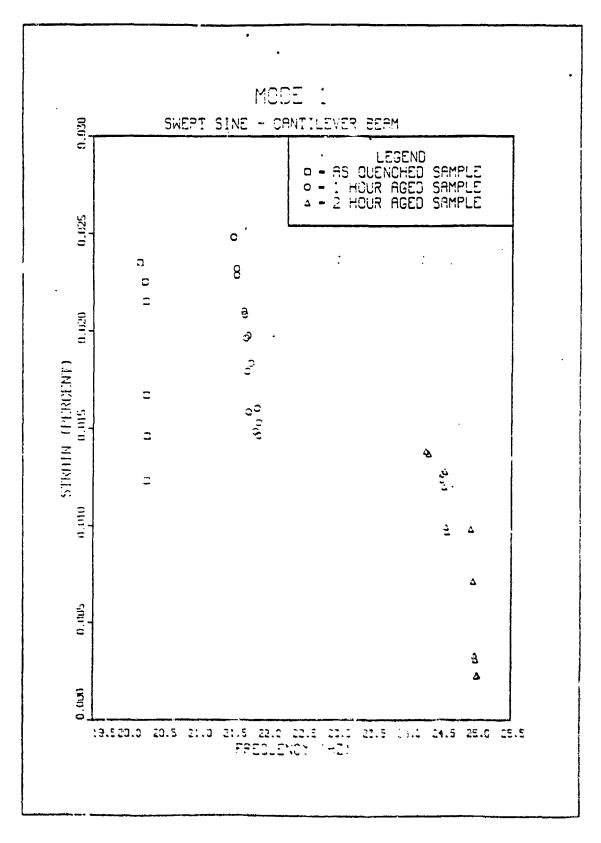


Figure 3.14 Mode 1 - Strain -vs- Frequency (Swept Sine)

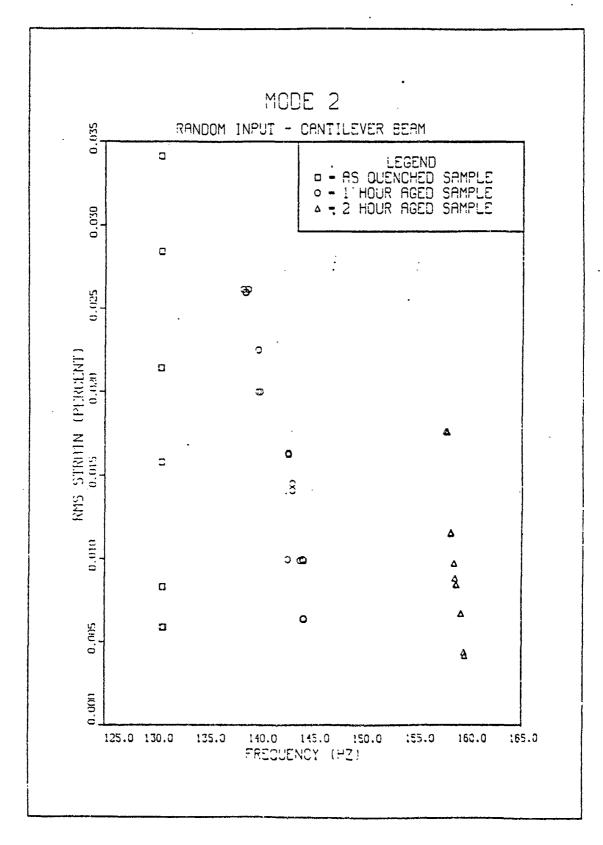


Figure 3.15 Mode 2 - Strain -vs- Frequency (Random Input)

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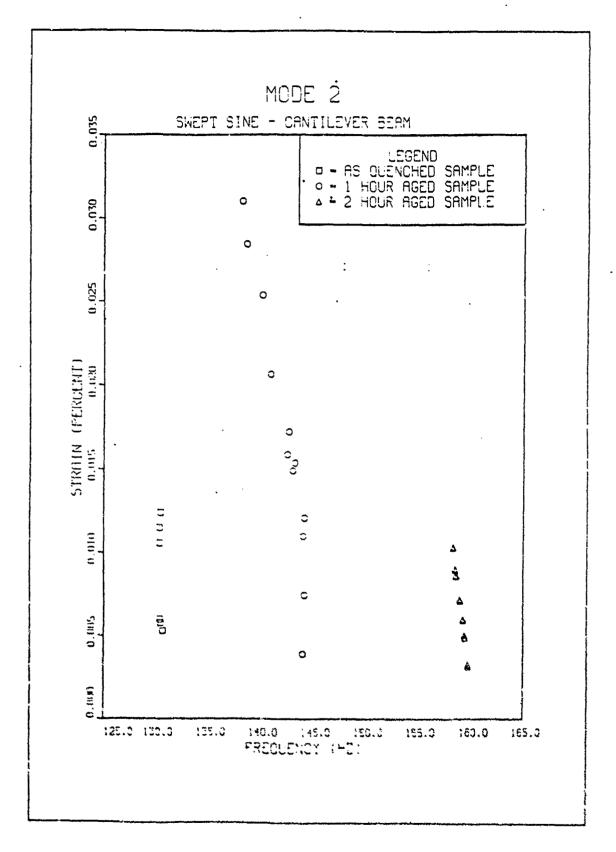


Figure 3.16 Mode 2 - Strain -vs- Frequency (Swept Sine)

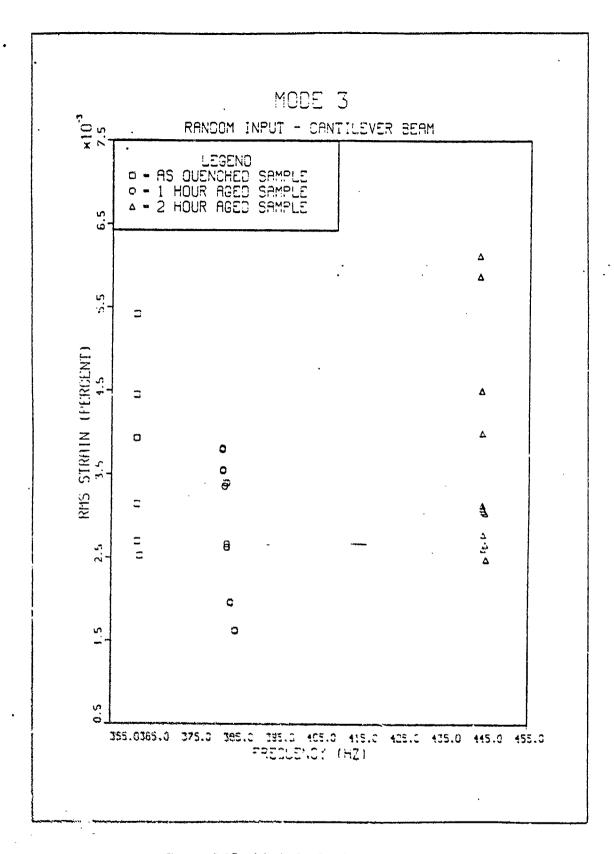


Figure 3.17 Mode 3 - Strain -vs- Frequency (Random Input)

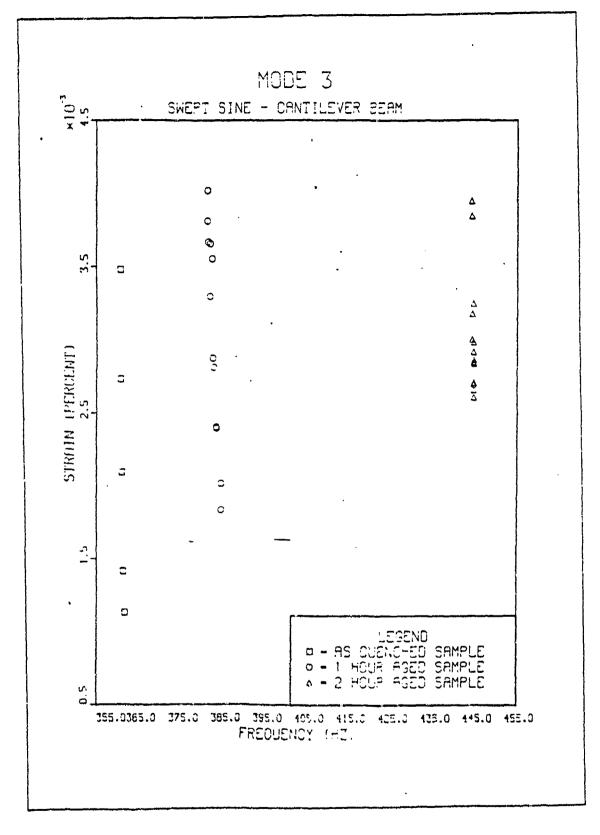


Figure 3.18 Mode 3 - Strain -vs- Frequency (Swept Sine)

E. INPUT ACCELERATION -VS- FREQUENCY

Figure 3.19 is a graph of the mode 1 Input Acceleration -vs- Frequency for a random input. In this graph as the input acceleration level increases the resonant frequency shifts downward in the same manner as seen in the Strain -vs- Frequency graphs. Since it was found (Figures 3.1 to 3.6) that the input acceleration and strain increase in a linear fashion and that an increase in strain corresponds to a decrease in resonant frequency, the downward shift of the resonant frequency with increasing input acceleration should occur in a similar fashion as it does with increasing strain. This downward shift does in fact occur. Figure 3.20 is the mode 1 Input Acceleration -vs-Frequency results using the swept sine input. This graph shows the same trend. In both cases, as aging time increases, the resonant frequency shifts downward faster. Figures 3.21 and 3.22 are the mode 2 results. Again, the resonant frequency shifts downward with an increase in the input acceleration level. In mode 2 it appears that the 1 hour aged sample makes the fastest frequency shift. This was seen earlier in the Strain -vs- Frequency graphs (Figures 3.15 and 3.16). Figures 3.23 and 3.24 are the mode 3 results. These results are comparable to the mode 3 results of Strain -vs-Frequency as they should be given the linear relationship between strain and input acceleration. As the excitation level is increased the resonant frequency shifts downward due to the change in Young's Modulus.

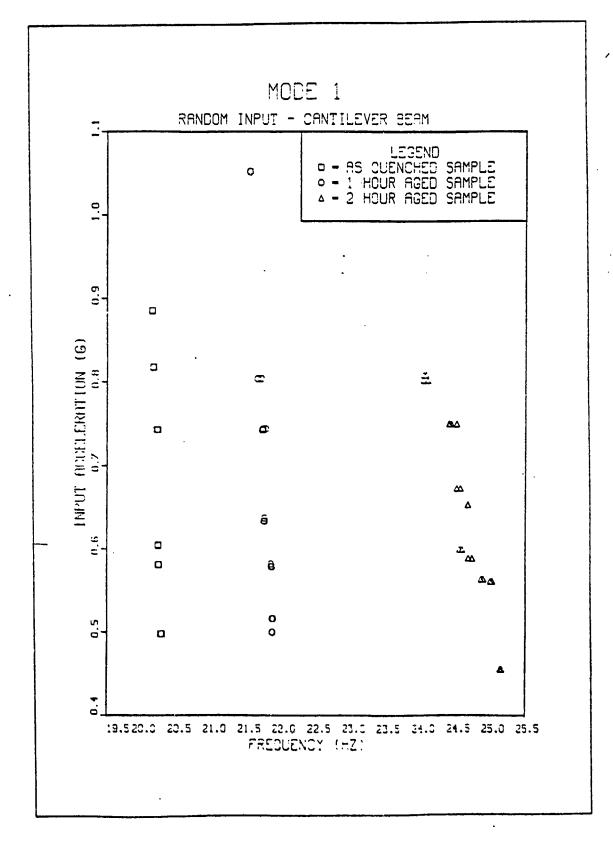


Figure 3.19 Mode 1 - Input Acceleration -vs- Frequency (Random Input)

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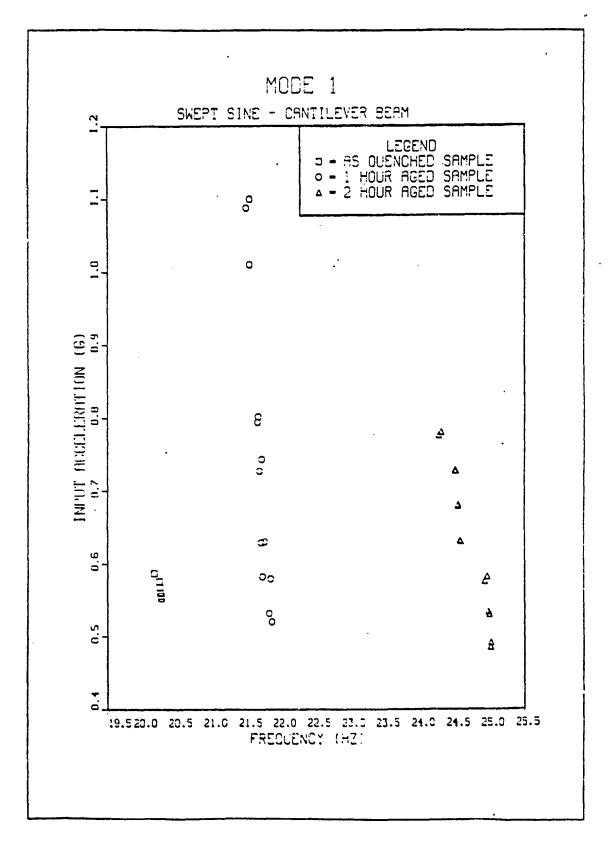


Figure 3.20 Mode I - Input Acceleration -vs- Frequency (Swept Sine)

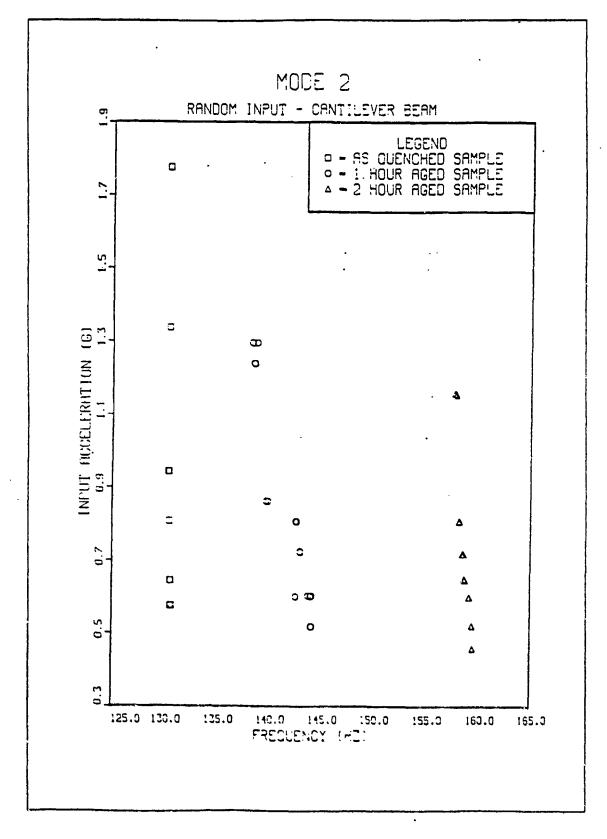


Figure 3.21 Mode 2 - Input Acceleration -vs- Frequency (Random Input)

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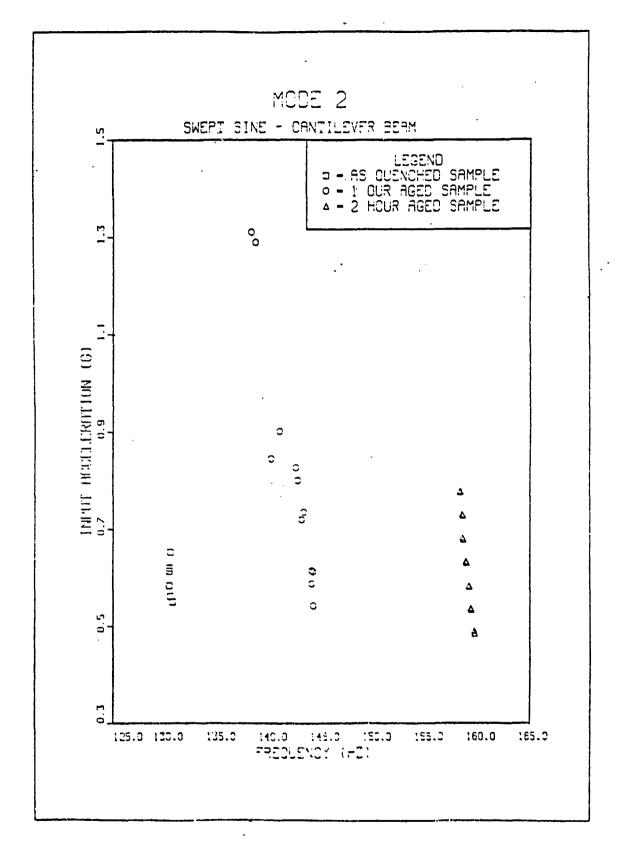


Figure 3.22 Mode 2 - Input Acceleration -vs- Frequency (Swept Sine)

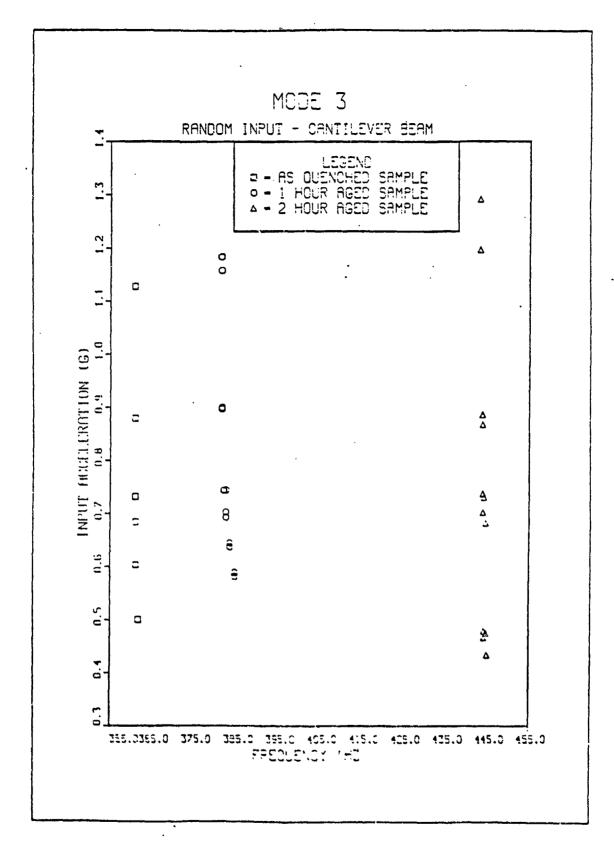


Figure 3.23 Mode 3 - Input Acceleration -vs- Frequency (Random Input)

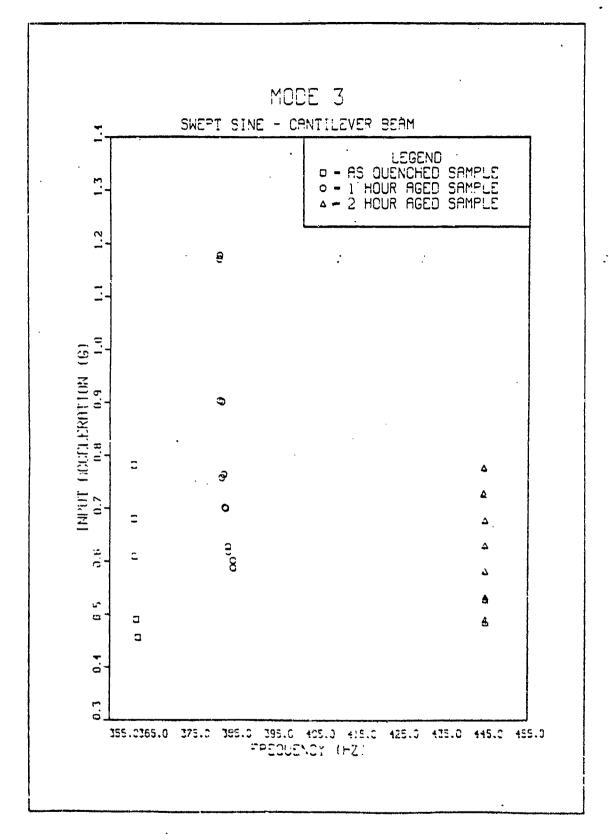


Figure 3.24 Mode 3 - Input Acceleration -vs- Frequency (Swept Sine)

F. INPUT ACCELERATION -VS- LOSS FACTOR

Figure 3.25 is the mode 1, random input graph of Input Acceleration -vs- Loss Factor. This graph shows that as the input acceleration is increased the loss factor of the material increases. Also, as the aging time increases the loss factor increases significantly. These two trends are exactly the same as the trends found in the Strain -vs- Loss Factor graphs. Once again this should occur since the strain and input acceleration can be related. The 2 hour aged sample shows a significant increase in loss factor as the input acceleration level reaches the 0.8g level. This could be a result of the non-linearities in the material. As mentioned in Chapter 1 the loss factor of the Mn-Cu material increases as aging time increases up to about 8 hours. Figure 3.26 is the swept sine graph of the input acceleration and loss factor for mode 1. As with the random input test, the loss factor increases with both increased input acceleration and increased aging time. The 2 hour aged samples show the same rapid increase in loss factor at an input acceleration level of 0.8g as it did in the random test. For complete analysis of the material this would involve further investigation but for this paper what is significant is the fact that the trend was occured in both the random input and swept sine tests. Figure 3.27 and 3.28 are the mode 2 results while Figures 3.29 and 3.30 are the mode 3 results. In mode 2 it appears that the loss factor of the 1 hour aged sample increases faster than the 2 hour aged sample. However, the general trend, that the loss factor increases with both increased input acceleration and increased aging time still holds. It can be seen that the highest loss factors are obtained in the first mode.

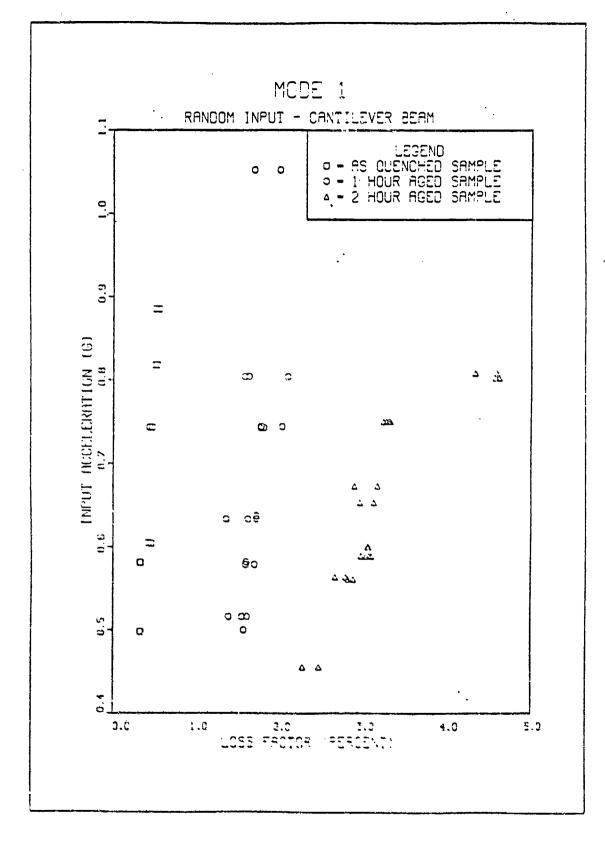


Figure 3.25 Mode 1 - Input Acceleration -vs- Loss Fance (Random Input)

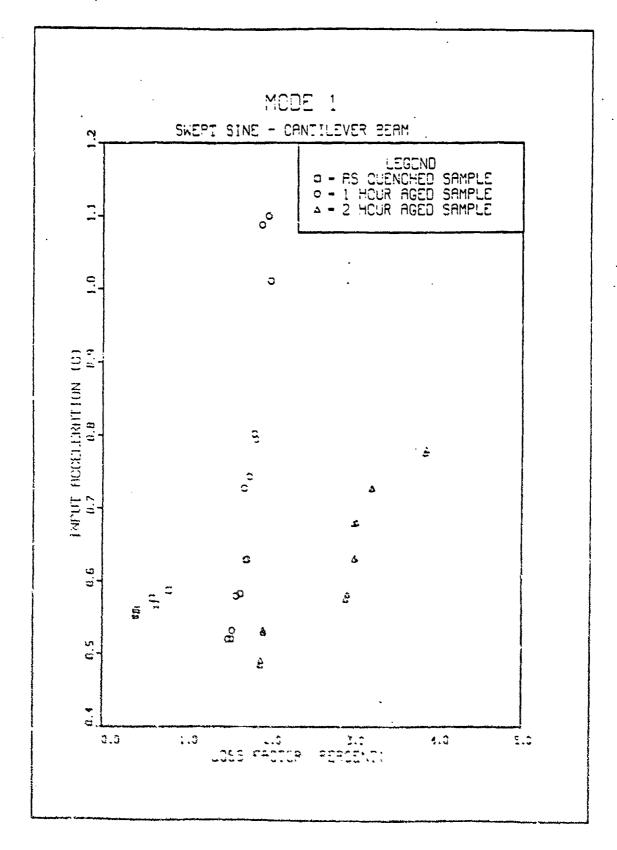


Figure 3.26 Mode I - Input Acceleration -vs- Loss Factor (Swept Sme)

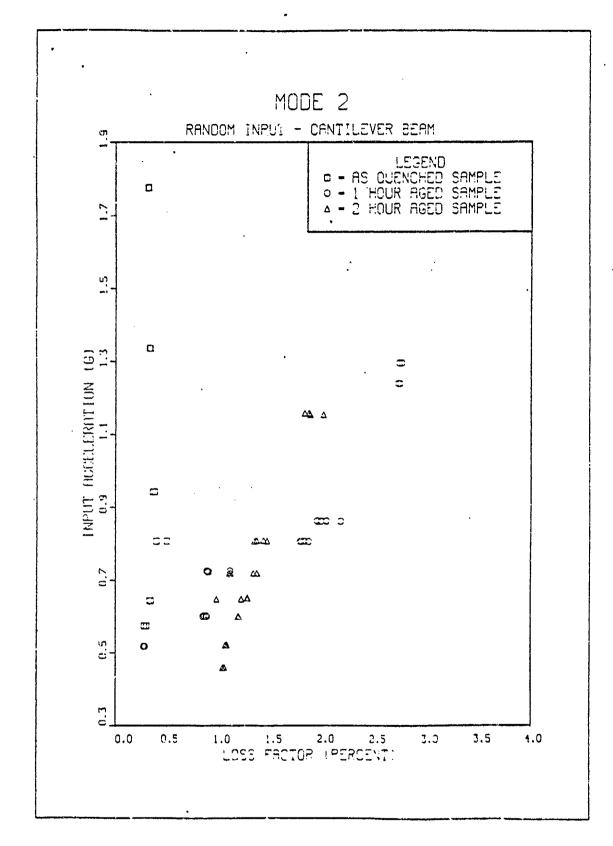


Figure 3.27 Mode 2 - Input Acceleration -vs- Loss Factor (Random Input)

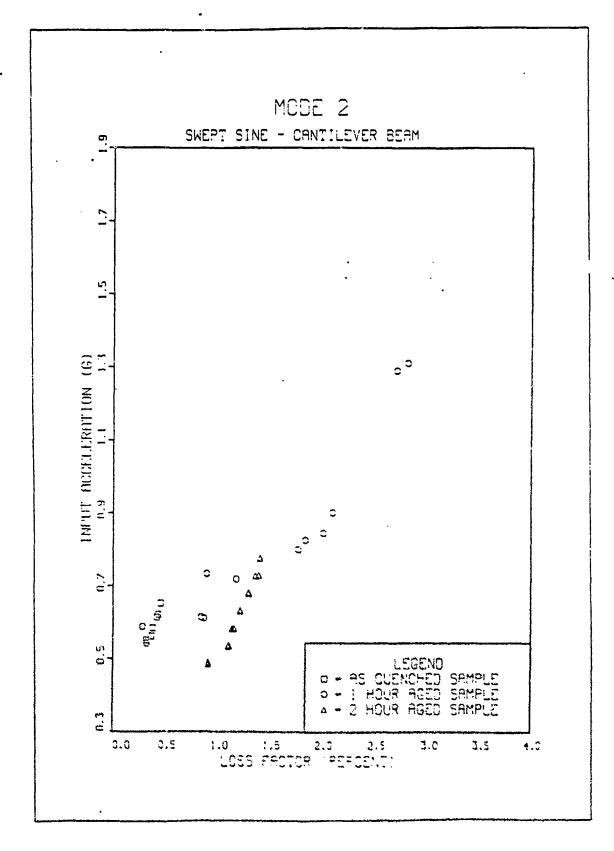


Figure 3.28 Mode 2 - Input Acceleration -vs- Loss Factor (Swept Sine)

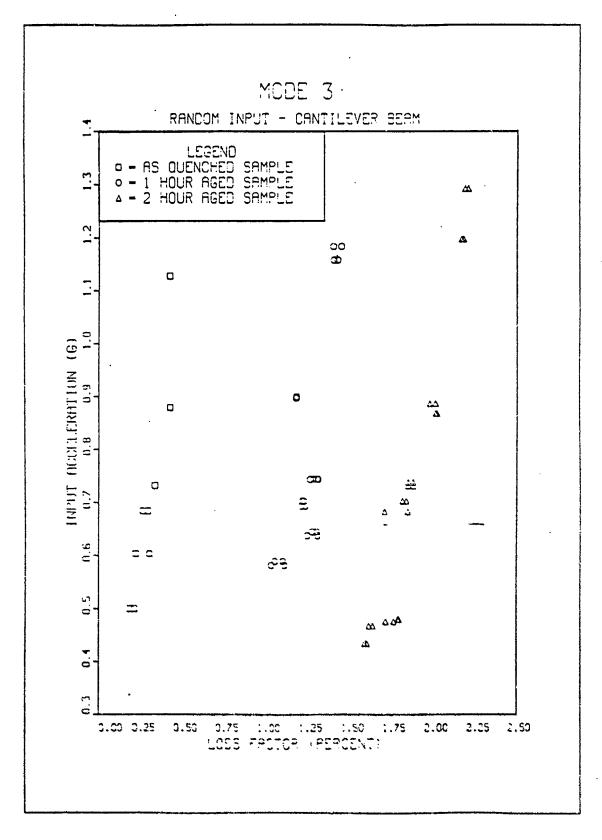


Figure 3.29 Mode 3 - Input Acceleration -vs- Loss Factor (Random Input)

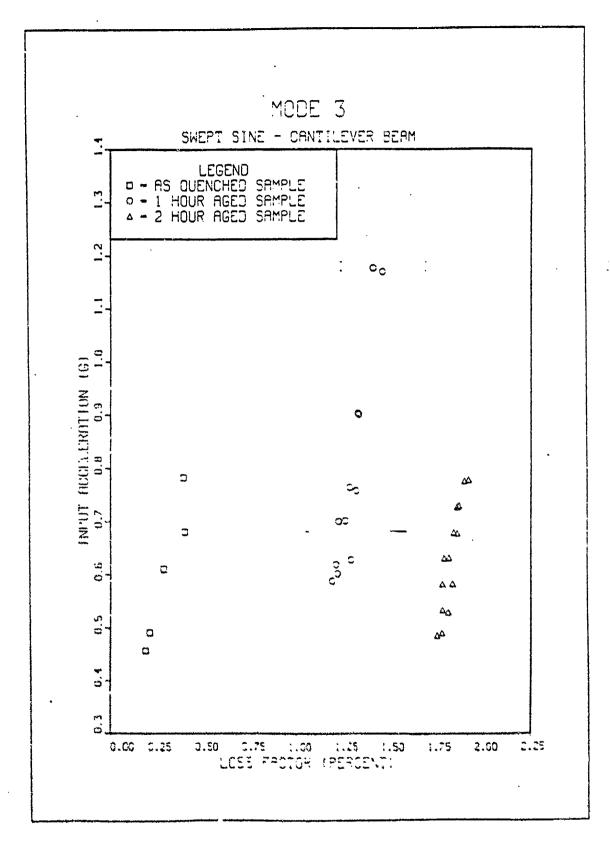


Figure 3.30 Mode 3 - Input Acceleration -vs- Loss Factor (Swept Smc)

G. LOSS FACTOR -VS- FREQUENCY

Figure 3.31 is a graph of the mode 1 random input results of the Loss Factor -vs-Frequency. This graph shows a linear relationship between the loss factor and the frequency. As the loss factor increases the resonant frequency shifts downward. This makes sense since an increase in the loss factor corresponds to an increase in the the amount of strain that the sample undergoes. As mentioned previously, an increase in the strain results in a decrease in the Young's Modulus of the material with a resulting decrease in the resonant frequency. Figure 3.32 is the mode 1 swept sine results. The two graphs are very similar indicating that either way of testing (using random input or swept sine input) will obtain good results. Figures 3.33 and 3.34 are the mode 2 results. In both of these graphs the relationship between the loss factor and frequency appears to be linear as it does in Figures 3.35 and 3.36 which are the mode 3 results.

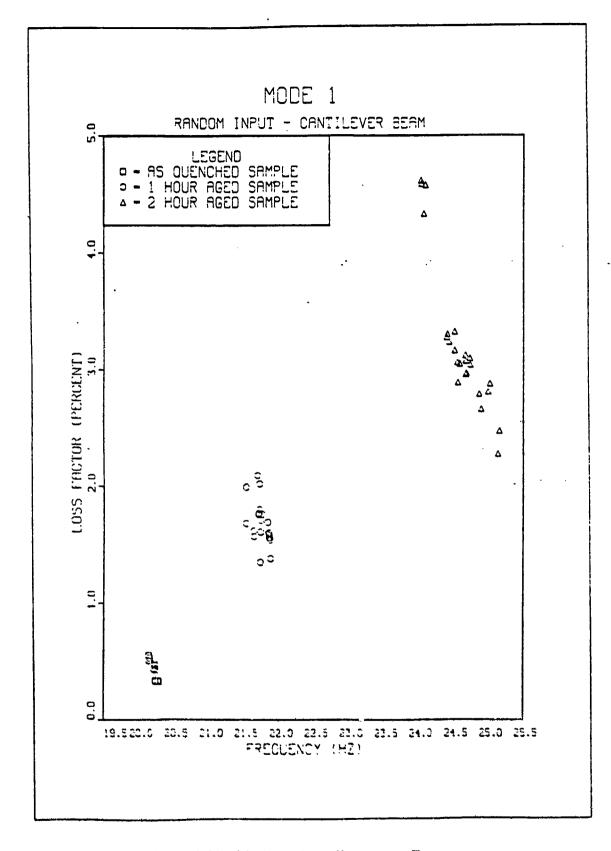


Figure 3.31 Mode 1 - Loss Factor -vs- Frequency (Random Input)

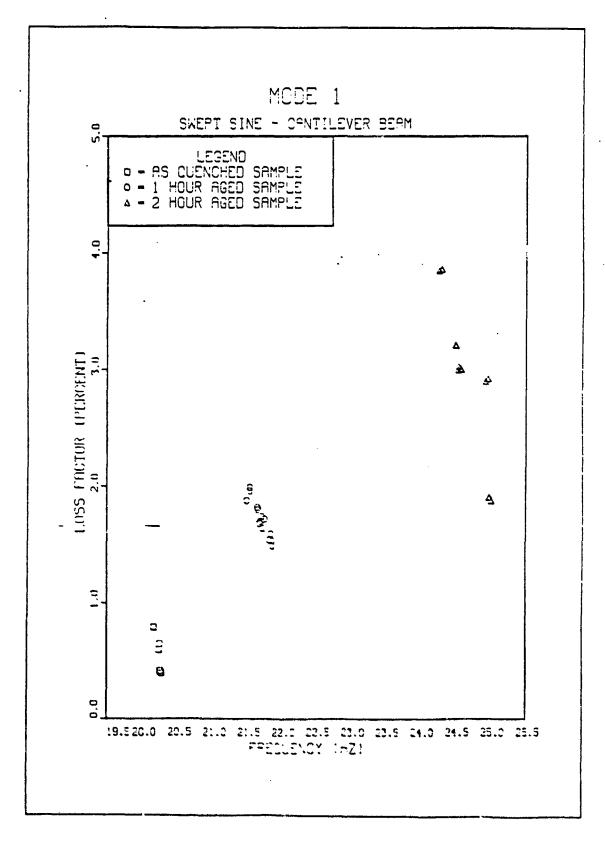


Figure 3.32 Mode 1 - Loss Factor -vs -Frequency (Swept Sine)

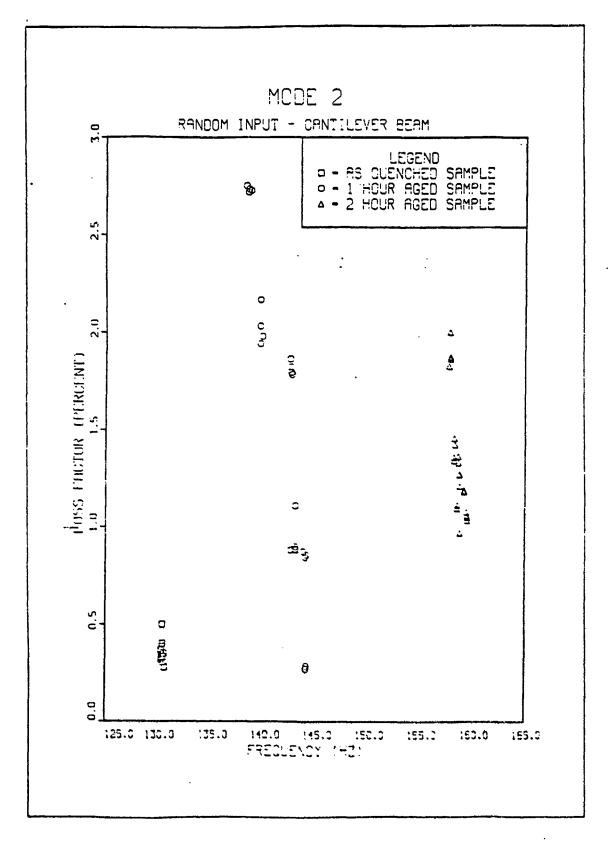


Figure 3.33 Mode 2 - Loss Factor -vs- Frequency (Random Input)

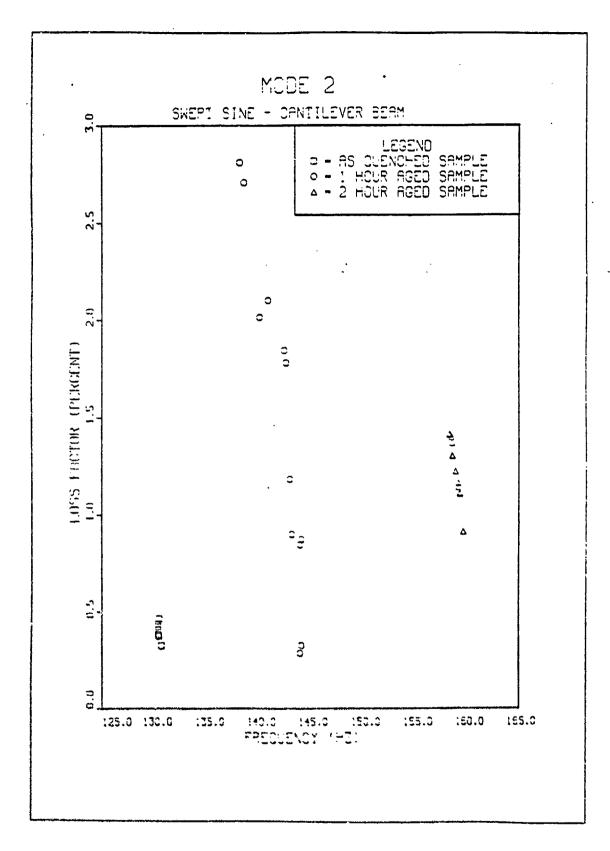


Figure 3.34 Mode 2 - Loss Factor -vs- Frequency (Swept Sine)

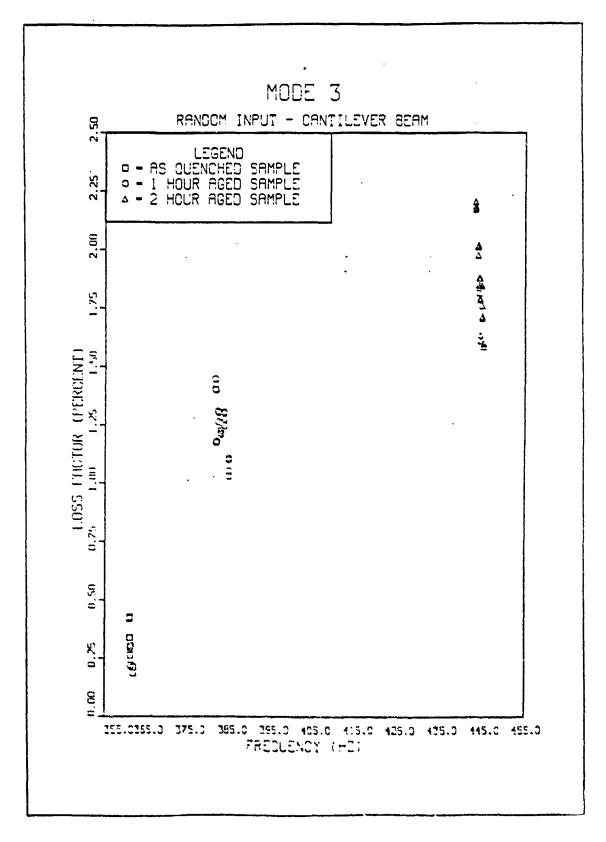


Figure 3.35 Mode 3 - Loss Factor -vs- Frequency (Random Input)

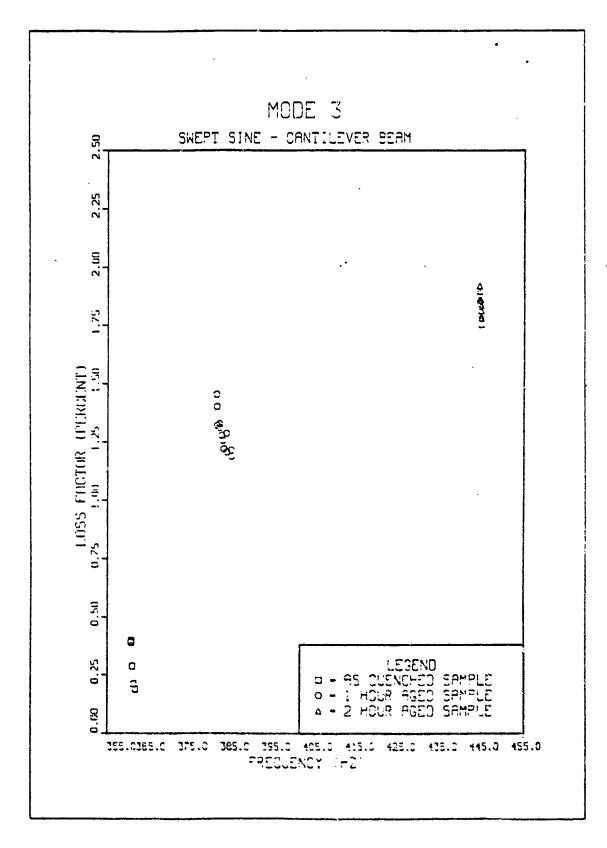


Figure 3.36 Mode 3 - Loss Factor -vs- Frequency (Swept Sine)

H. DISCUSSION

In running the tests some problems were encountered. The strain gages have a fatigue life of approximately 10⁵ cycles. The fatigue is a function of the solder joint formation. Since the first mode has the highest tip deflection it is recommended that this mode be tested after the third and second modes. To prevent inadvertent joint damping the sample should be securely tightened and once it is placed in the test stand it should not be removed until after all desired testing has been performed. Both the strain gages and the accelerometers can be a source of extraneous noise if their associated wiring is allowed to repeatedly hit the beam sample as it vibrates. In this investigation the accelerometer coaxial cable (tip accelerometer only) was taped along the cantilever beam. Also the strain gage wiring was taped to the beam right after the gage solder connection. The wire was then looped to allow free vibration of the beam without any interference. This scotch tape could have an effect on the damping, however, considering the small amounts of tape used it was felt that this did not contribute significantly to the damping. Using large accelerometers on the tip will mass load the system, causing the resonant frequency to shift significantly downward (on the order of 5-10 Hz). The time to run the tests varied greatly between the random input and swept sine input tests. For one cantilever beam, to investigate all three modes, required almost 25 hours using the random input source. This compared to 5 hours using the swept sine source. The coherence for both tests was very good although measuring the strain and input acceleration for the swept sine tests was more difficult since the strain and acceleration are constantly changing. The swept sine tests compare favorably with the random tests. Therefore, either test could be used when comparing different materials, provided that the test samples have the same geometry. For lower levels of strain the random input tests give better results since the swept sine signal-to-noise ratio is very small making measurements of strain and damping difficult. Higher levels of strain can be obtained using the swept sine input method. Using swept sine input for higher strain levels and random angur for lower strain levels would give satisfactory results.

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IV. TORSION SAMPLE EXPERIMENTAL METHOD

A torsion testing apparatus was constructed to enable testing of the Sonction specimen in torsion (Appendix C). The specimens were designed such that they form a single degree of freedom system under base excitation. Therefore, unlike the cantilever beam, where the strain varies along the beam length, the shear strain is constant at the cuter radius along the length of the sample shaft. Appendix B delineates how the natural frequency of such a system can be calculated. In this test the sample was a 12 cm. long cylinder with a 0.8 cm. diameter. The same three heat treatments were performed as for the cantilever beams: Solution Annealing at 800°C for 1 hour, water quenching, and then aging one sample for 1 hour at 425°C; aging one sample for 2 hours at 425°C; and leaving one sample unaged. A strain gage was attached to allow for determining the shear strain that the specimen undergoes. Two Endevco accelerometers were used to obtain the transfer function between the base and the end rotation of the cylinder. The first accelerometer was attached to the turning disc while the second was attached to the heavy mass on the end of the sample. Figures 4.1 and 4.2 are photos of the torsion test apparatus and torsion sample respectively.

For random input testing, the RMS Shear Strain level was determined in exactly the same manner as it was for the bending strain (the average of ten 5mSec time samples for each excitation level). Figure 4.3 is a representative time history of one shear strain variation during a random test. The RMS input acceleration level was also obtained by averaging ten 5mSec time samples (Figure 4.4). An initial transfer function from 0-200 Hz using a random input was performed on the unaged sample in order to make sure that the sample was only excited in the torsion mode (Figure 4.5). A 60 Hz spike occurs every time, however. Baseband tests were also run for the Ihour and 2 hour samples. The torsion and bending frequencies were calculated using the values of Young's Modulus obtained from the tensile tests performed (refer to Chapter 2) and compared to the value obtained by zooming the test near the resonant frequency region. The Half-Power Point Method was us d for determining the loss factor from the transfer function. In all three cases only the torsion mode was excited. Each sample was analyzed at nine different amplification levels

For the swept sine tests, measurements of it put acceleration and shear strain were made in the same way except that the time domain data was obtained at the peak of the transfer function. Six different amplification levels were used in the swept sine tests.

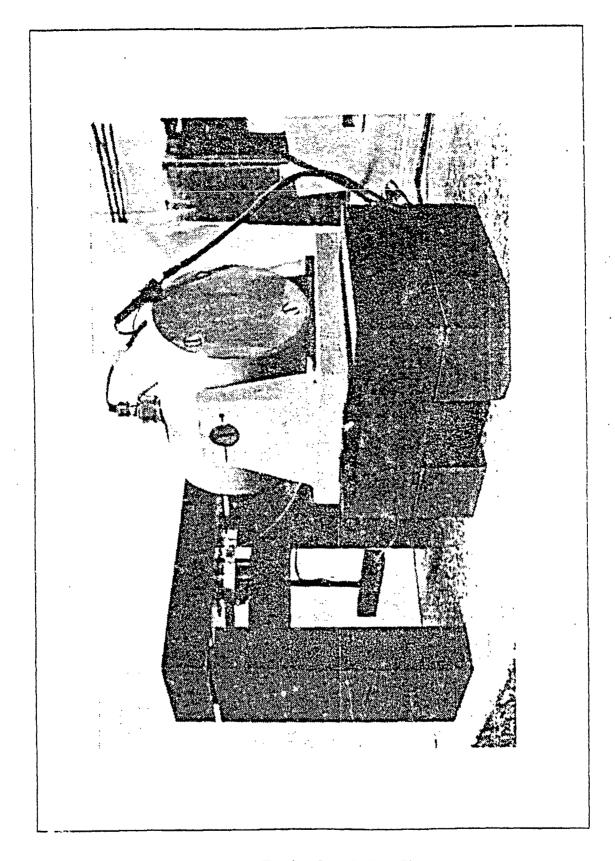


Figure 4.1 Torsion Sample Test Fixture

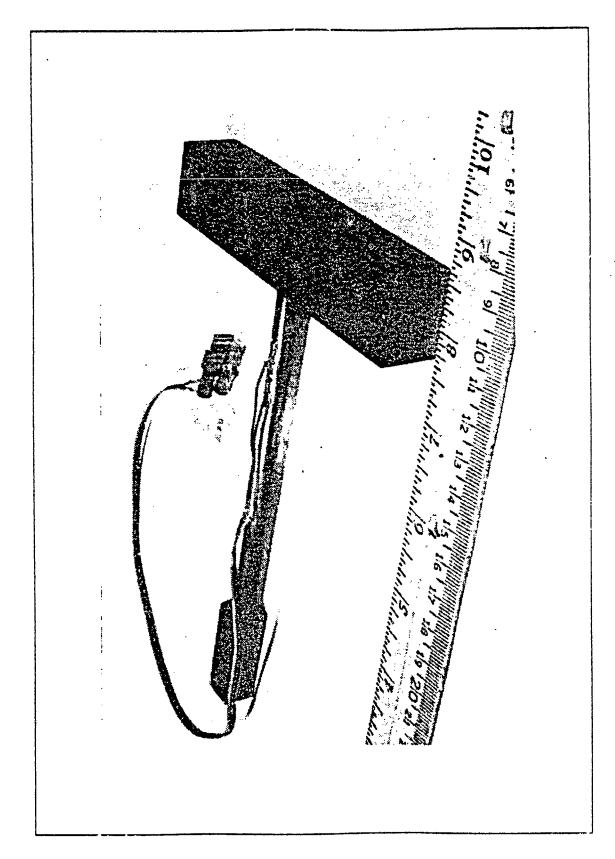


Figure 4.2 Torsion Sample Photograph

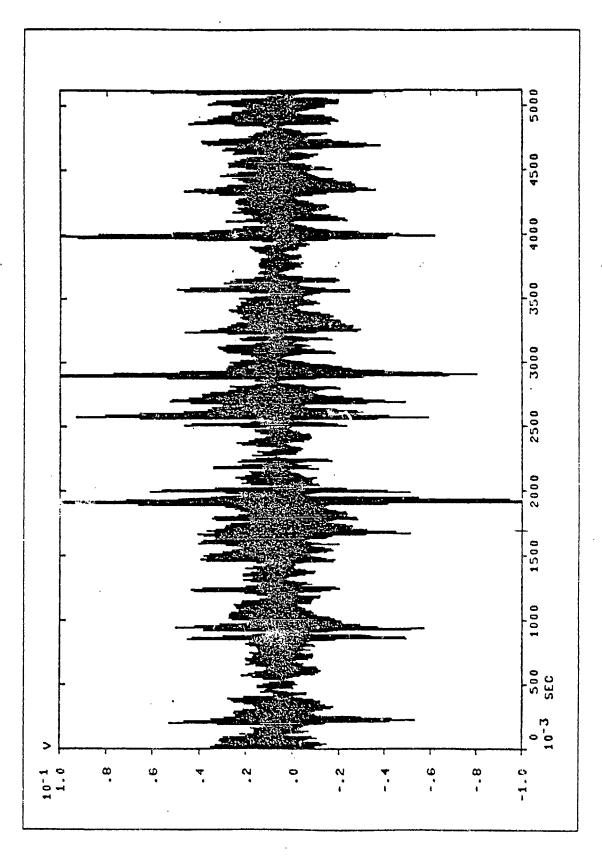


Figure 4.3 Time Sample of Shear Strain Gage

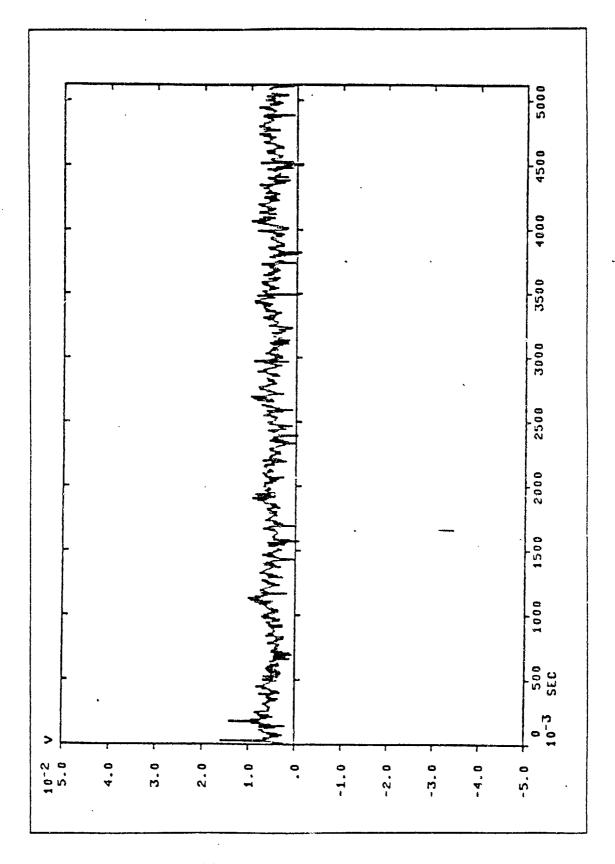


Figure 4.4 Time Sample of Torsion Input Accelerometer

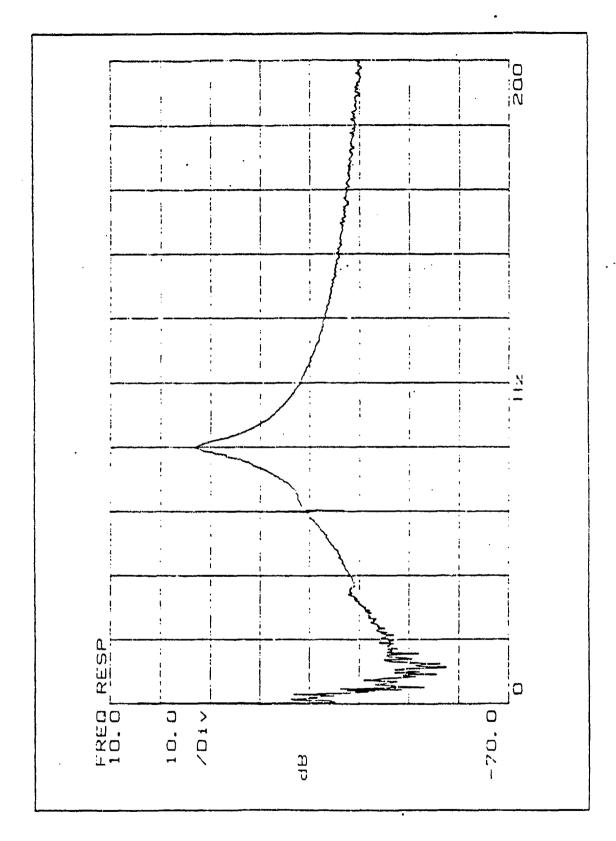


Figure 4.5 Baseband Response for Solution Annealed Sample

V. TORSION SAMPLE RESULTS AND DISCUSSION

A. GENERAL

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The torsion samples that were analyzed give results in the frequency range 65-85 Hz. The solution annealed sample has a resonant frequency of 83 Hz compared to the calculated value of 84.5 Hz. For the 1 hour and 2 hour aged samples the calculated values were 89.6 and 101.9 Hz respectively but the actual resonant frequencies were approximately 68 Hz for both. The calculations were based on the values of Young's Modulus obtained from the tensile tests (Chapter 2) and assumed that the material was isotropic. Part 2 of Appendix D shows a representative transfer function (both in log magnitude and linear scales) for 32 time averages of one torsion sample. It also shows the 180° phase shift and coherence function associated with this one torsion test. The collected data from the random input and swept sine tests are listed in Appendix E, part 2.

B. INPUT ACCELERATION -VS- SHEAR STRAIN

Figure 5.1 shows the Input Acceleration -vs- RMS Shear Strain for a random input. This RMS shear strain value is determined exactly in the same manner as it was for the cantilever beam in Chapter 2. The input acceleration also is obtained in this manner. Each sample was tested at 9 different amplification levels with each value of strain and acceleration representing the average value of ten time samples. In this test the shear strain increases with increasing input acceleration in a linear fashion except at the highest levels of input. Figure 5.2 also is a graph of Input Acceleration -vs-Shear Strain but with a swept sine input instead of a random input signal. In this case the shear strain is obtained at the resonant frequency as is the value for the input acceleration (discussed in Chapter 2). The same trend exists between the shear strain and input acceleration using the swept sine input as it did for the random input. In both figures the shear strain increases with aging time, however, the 1 and 2 hour aged samples have very similar results indicating that when tested in the torsion mode the differences in aging times may not be as important as it is in the bending mode.

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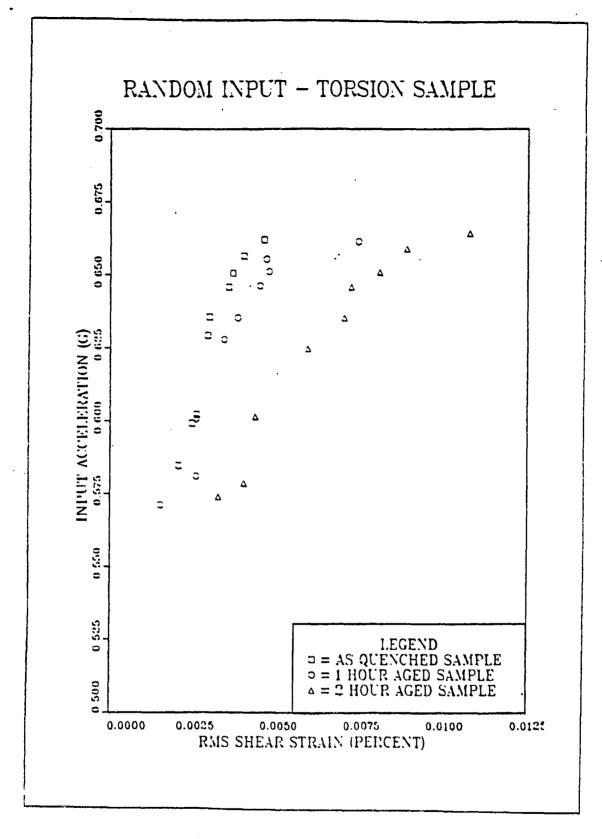


Figure 5.1 Torsion - Input Acceleration -vs Shear Strain (Random Input)

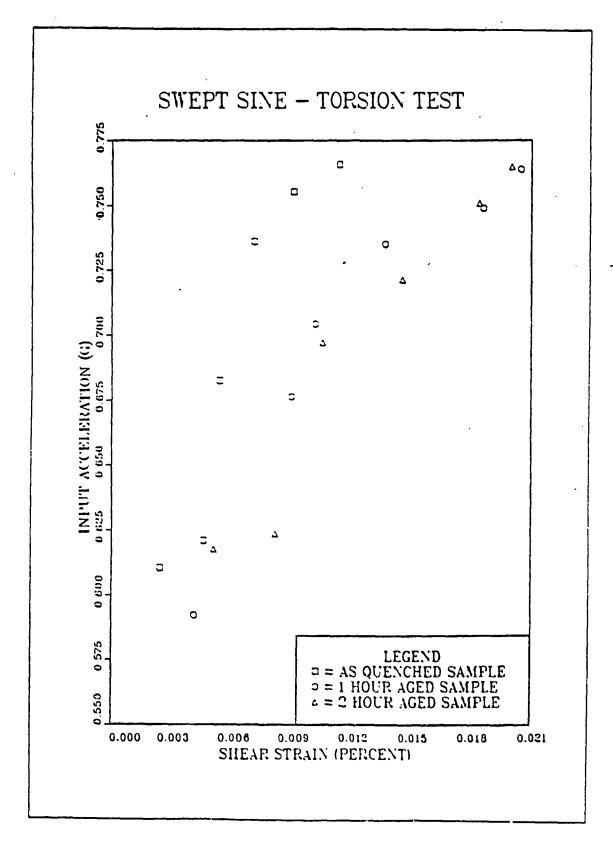


Figure 5.2 Torsion - Input Acceleration -vs- Shear Strain (Swept Sine)

C. LOSS FACTOR -VS- SHEAR STRAIN

Figure 5.3 shows the Loss Factor -vs- RMS Shear Strain for random input. The results are similar to those found for the cantilever beam in that higher levels of strain produce higher loss factors and the loss factor increases with aging time. The results also show that the loss factor depends on shear strain and is very nonlinear for the aged samples. In the torsion case the 1 and 2 hour aged samples give fairly identical results. The torsion test was run a second time using a swept sine input (Figure 5.4). The results from this test are very similar to those of the random input test.

D. SHEAR STRAIN -VS- FREQUENCY

Figure 5.5 is a graph of RMS Shear Strain -vs- Frequency for random input. The resonant frequency shifts downward as the shear strain increases. An increase in shear strain corresponds to a decrease in the Shear Modulus just as an increase in bending strain corresponds to a decrease in Young's Modulus for the cantilever beam. This decrease in Shear Modulus results in a lower resonant frequency which is similar to the results obtained in the cantilever beam tests. Again the 1 and 2 hour aged samples give very similar results. When compared to Figure 5.5, the swept sine test results for Figure 5.6 gives approximately the same results.

E. INPUT ACCELERATION -VS- FREQUENCY

Figure 5.7 is a graph of the Input Acceleration -vs- Frequency for the random input test. As in the cantilever beam case the resonant frequency shifts downward as the input acceleration increases. In the torsion test this is due to the decrease in the Shear Modulus since the input acceleration is directly related to the shear strain. The frequency shift appears to be the same for all three samples. Figure 5.8 graphs the results of the swept sine tests. Again, the frequency shift downward appears although it is not quite as pronounced as with the random test.

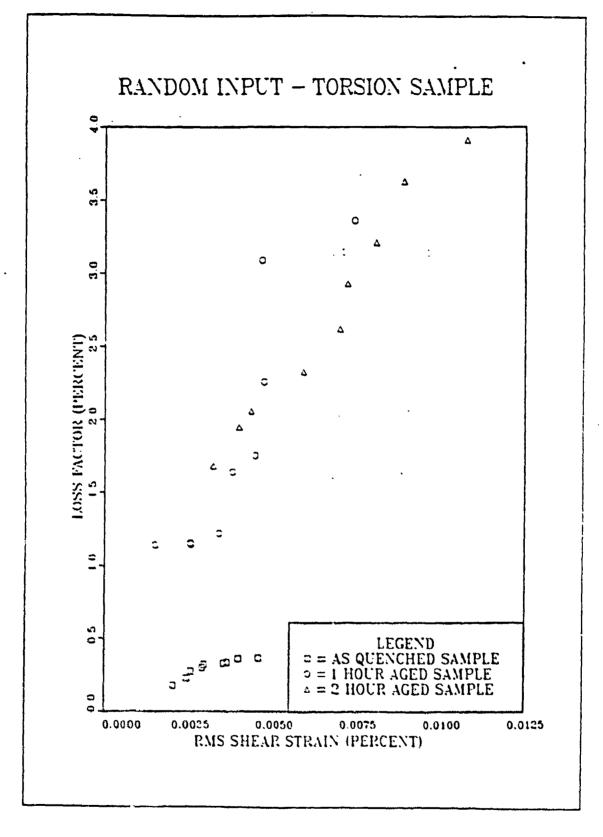


Figure 5.3 Torsion - Loss Factor -vs- Shear Strain (Random Input)

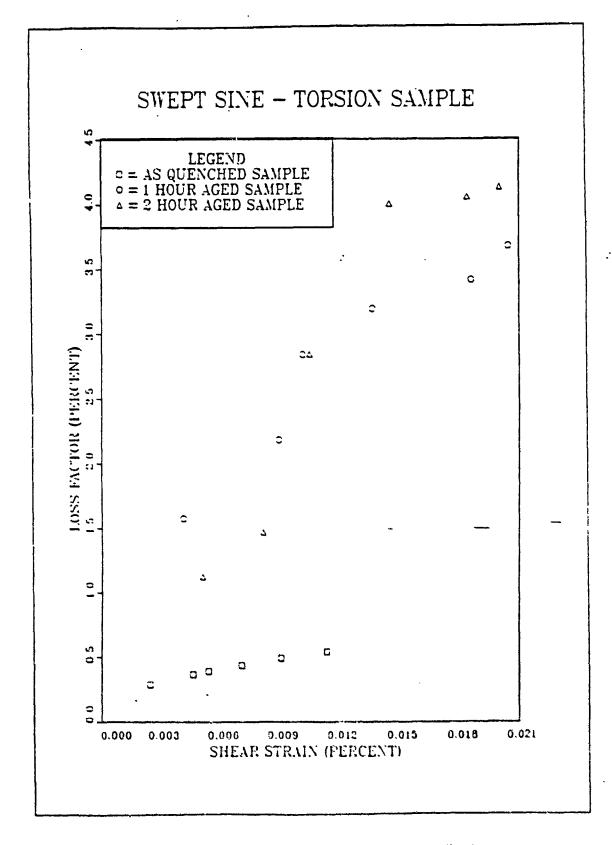


Figure 5.4 Torsion - Loss Factor -vs- Shear Strain (Swept Sine)

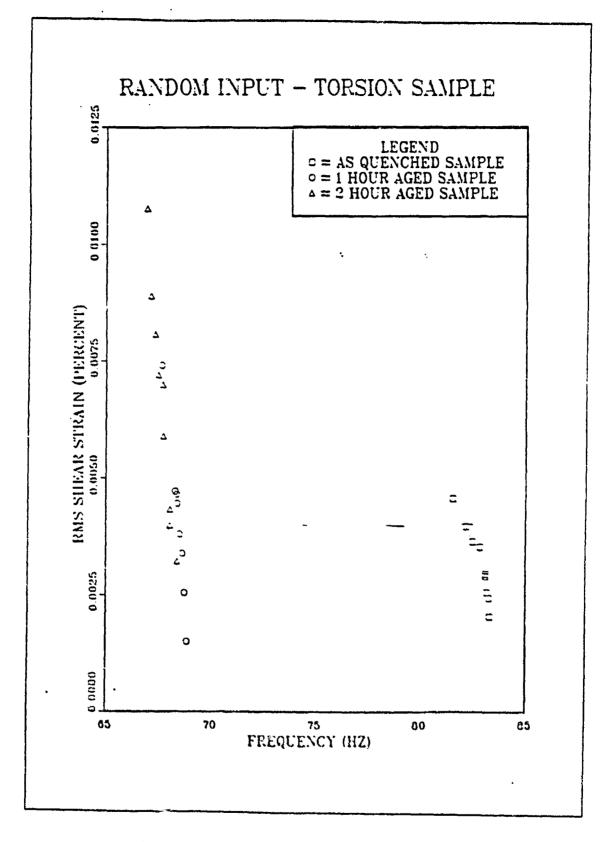


Figure 5.5 Torsion - Shear Strain -vs- Frequency (Random Input)

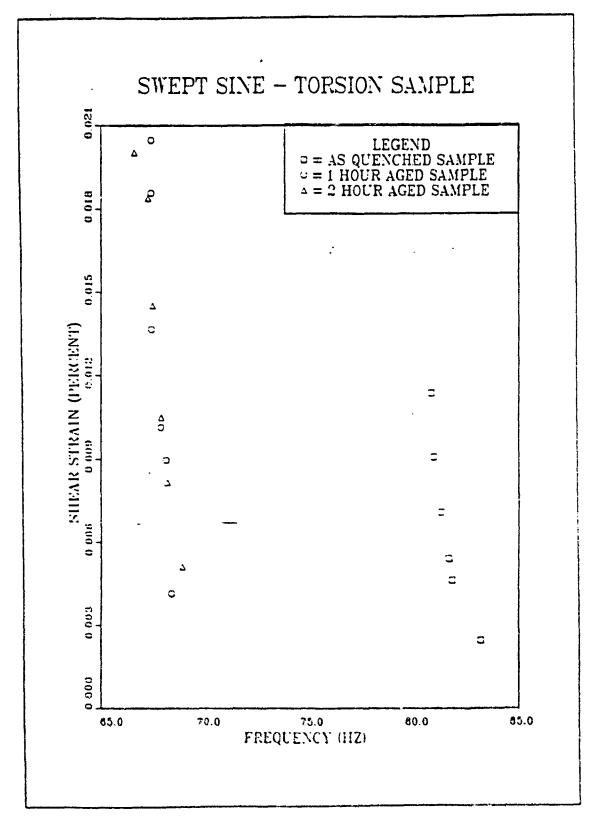


Figure 5.6 Torsion - Shear Strain -vs- Frequency (Swept Sine)

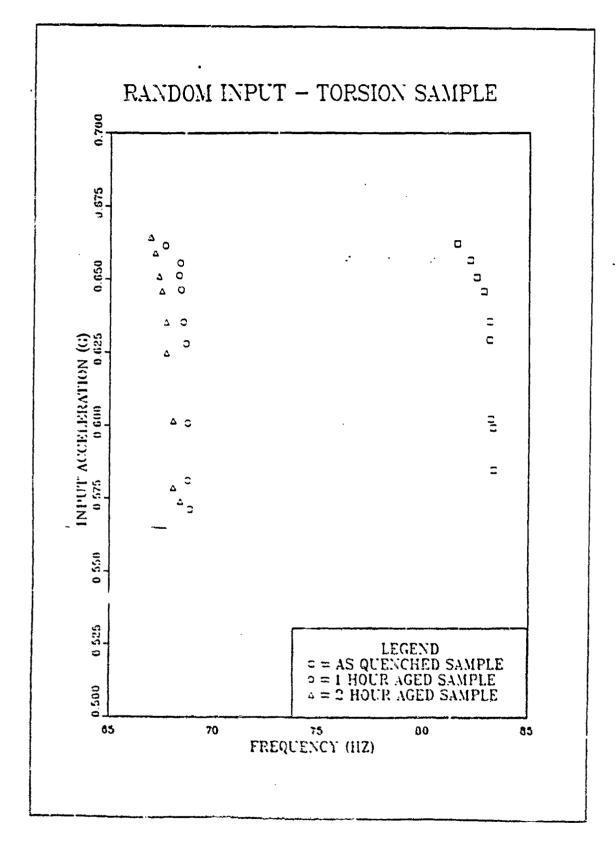


Figure 5.7 Torsion - Input Acceleration -vs- Frequency (Random Input)

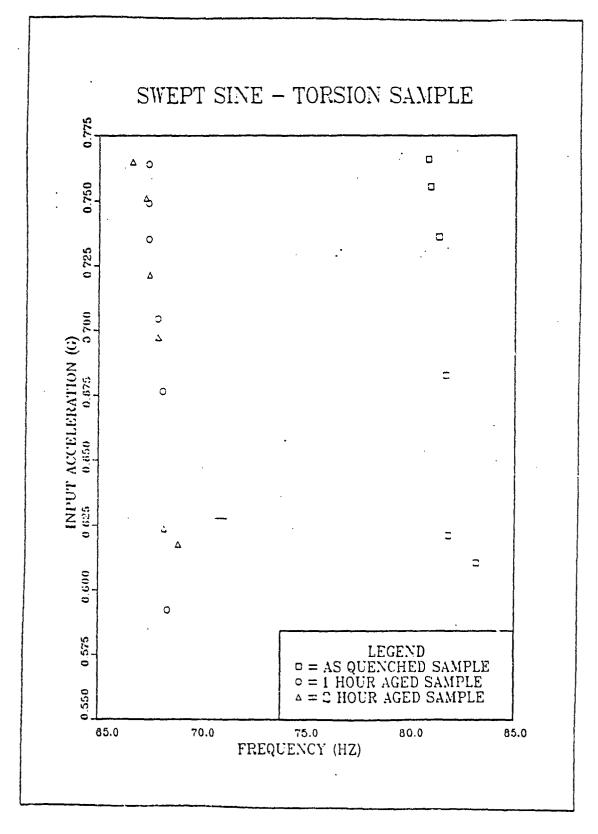


Figure 5.8 Torsion - Input Acceleration -vs- Frequency (Swept Sine)

F. INPUT ACCELERATION -VS- LOSS FACTOR

Figure 5.9 shows the loss factor as a function of the input acceleration. As with the results of Loss Factor -vs- Shear Strain the loss factor increases with both an increase in the input acceleration and with the aging time. The increase in the input acceleration corresponds to an increase in the shear strain and thus an increase in the loss factor. These results are similar to those for the Loss Factor -vs- Shear Strain and are expected. Aging time does play a part in increasing the loss factor but there does not seem to be much of a difference between the 1 hour and 2 hour aged samples when tested in the torsion mode. Figure 5.10 depicts the results of the swept sine tests. These results show a difference in the loss factor between the 1 and 2 hour aged samples although they do follow the same trend as the random input results.

G. LOSS FACTOR -VS- FREQUENCY

Figure 5.11 shows the resonant frequency as a function of the loss factor. As the loss factor increases, the resonant frequency shifts downward for all three samples. This shift is more pronounced for the unaged sample than for the 1 and 2 hour aged samples. The downward frequency shift is a result of an increase in shear strain and the resulting decrease in the Shear Modulus. This increase in the shear strain also causes the increase in the loss factor. Figure 5.12 is the swept sine results. These results are similar to the random input results, again indicating that testing of materials can be conducted using either random or swept sine input.

H. DISCUSSION

The swept sine test results compare favorably with those of the random input tests. Therefore, both tests could be used to compare different materials provided the same geometry was involved since the values obtained are shape dependent and not dependent on the material properties. For lower levels of shear strain the random tests give better results since the swept sine signal-to-noise ratio is very small making measurements of damping and shear strain difficult. Higher levels of shear strain can be obtained using the swept sine input method. Since both random and swept sine inputs give similar results, using swept sine input for higher measurement levels and random input for lower measurement levels gives satisfactory results.

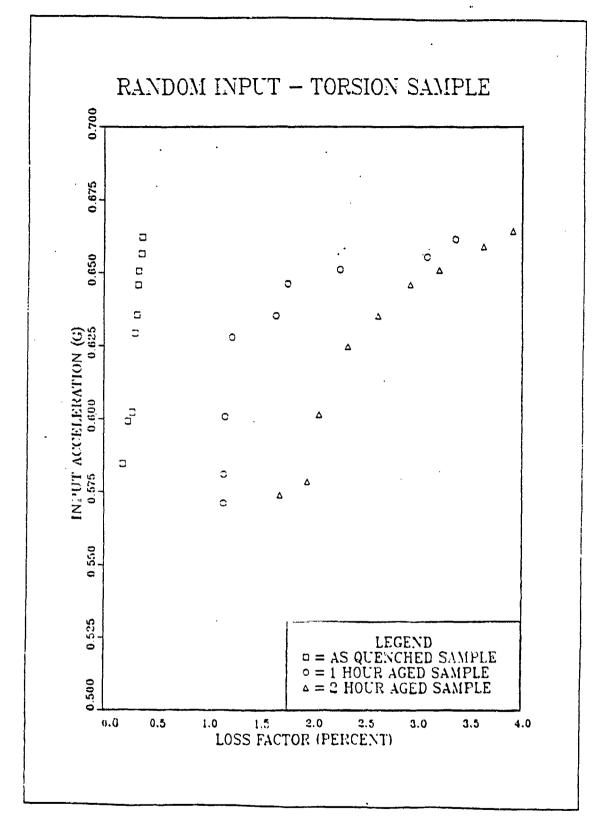


Figure 5.9 Torsion - Input Acceleration -vs- Loss Factor (Random Input)

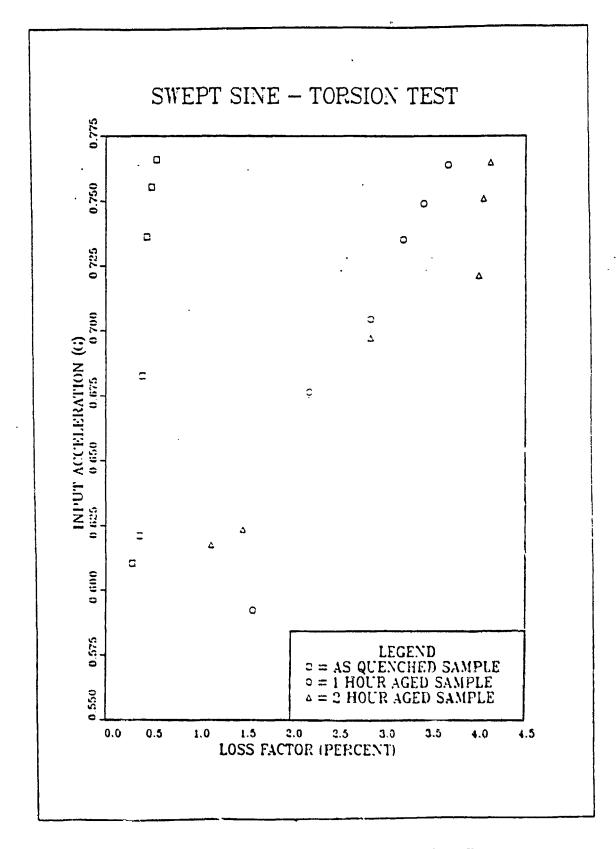


Figure 5.10 Torsion - Input Acceleration -vs- Loss Factor (Swept Sine)

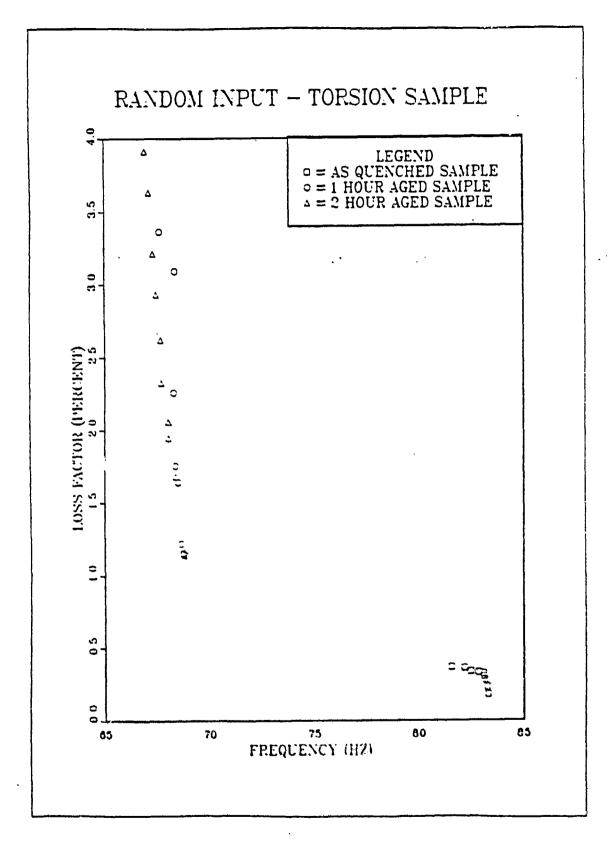


Figure 5.11 Torsion - Loss Factor -vs- Frequency (Random Input)

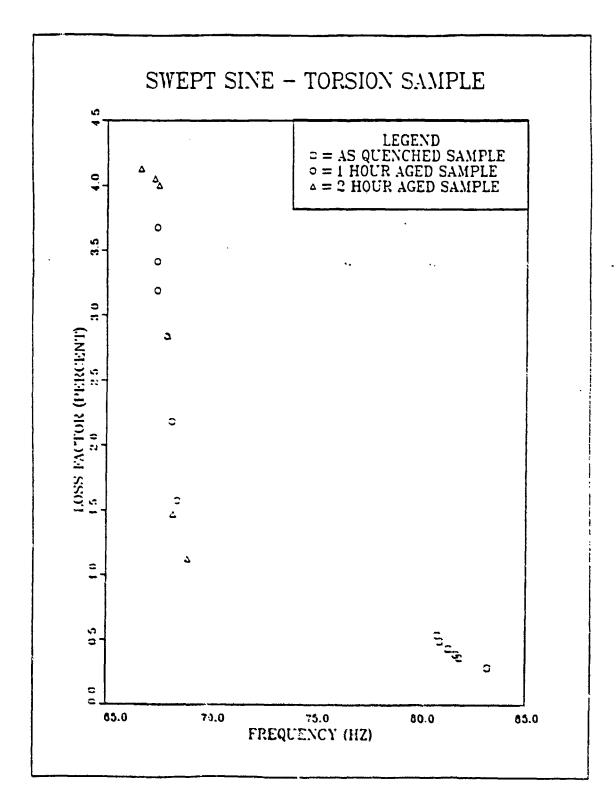


Figure 5.12 Torsion - Loss Factor -vs- Frequency (Swept Sine)

VI. DISCUSSION AND RECOMMENDATIONS

The results of the testing conducted on both the cantilever beam and torsion samples are repeatable whether random input is used for the excitation source or swept sine is used. In all of the cases the geometry of the samples to be compared must be the same in order for analysis of the different mechanical properties of the materials to be accomplished. As mentioned previously using a random input for lower levels of strain (bending or shear) gives better results since the swept sine signal-to-noise ratio is very small making measurements of the strain and damping difficult. The swept sine input should be used for higher levels of strain. Another consideration in deciding which test to run involves the amount of time available for analyzing the samples. The swept sine tests are much faster than the random tests, in this case it was approximately 5 times faster.

The following recommendations are provided to assist follow-on investigations:

- 1. Investigate higher strain levels. For the cantilever beam arrangement this would involve shorter length samples.
- 2. Investigate the use of multiple input excitation for the torsion setup. Using two identical vibration generators attached to the turning disc on opposite sides would prevent any possibility of inadvertently electing a bending mode. This would allow higher levels of shear strain to be obtained.
- 3. Investigate specimens with longer aging times.
- 4. Use of a non-contacting excitation scheme would get rid of any damping due to the shaker contacting the sample.

APPENDIX A HALF-POWER POINT METHOD

Physical systems usually have small values of damping. It is common to find systems with gain factors having sharp peaks and phase factors showing rapid 180° phase shifts. The system, therefore looks like a narrow bandpass filter, with bandwidth measured in terms of the half-power point bandwidth of the frequency response. These half-power points (Figure A.1) are located at a point .707 of the amplitude of the resonant frequency (ω_n) . The bandwidth is then defined as $(\omega_2-\omega_1)/(\omega_n)=(f_2-f_1)/f_n=2\xi$. The quality factor, Q, which is a measurement of the sharpness of resonance, is also easily obtained by:

$$Q = f_{n}/(f_{2}-f_{1}) = 1/2\xi$$
(A.1)

If the amplitude is measured in decibels then the half-power points correspond to a 3 db loss from the peak.

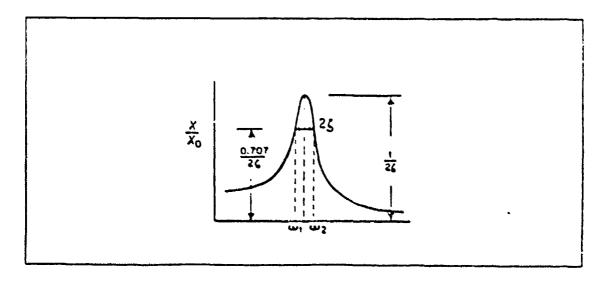


Figure A.1 Half-Power Point Method (Ref. 8)

APPENDIX B

DETERMINATION OF NATURAL FREQUENCIES

1. CANTILEVER BEAM

The differential equation for the lateral vibrations of a cantilever beam comes from Euler's equation for beams. Reference 8 gives a good explanation of how to obtain the resonant frequency of a beam which is determined from:

$$\omega_{n} = A\sqrt{(E1)/(\mu I^{4})} \tag{B.1}$$

Table B.1 lists values of A for different beam configurations and modes of vibration. In this study the first three modes of the cantilever beam have values for A of 3.52,22.4,and 61.7. The moment of inertia (I) of the beam is found by the equation (1/12)bh³ For the beams in this experiment: (Figure B.1)

length(1) = 7.5 inches

$$\mu = 41.408 \times 10^{-6} (lb\text{-sec}^2)/(in.^2)$$

width(b) = 0.5 inches
thickness(h) = 1.16 inch
 $I = 10.1725 \times 10^{-6} (in.^4)$

The calculated resonant frequencies for the samples tested in this experiment are listed in Table B.2.

TABLE 1 **VALUES OF A FOR DIFFERENT BEAM CONFIGURATIONS**

BEAMS OF UNIFORM SECTION AND UNIFORMLY DISTRIBUTED LOAD AMOULAR NATURAL FREQUENCY *** *** \$\frac{1}{x^{1}}\$ RAD/SEC

{Ref. 8}

WHERE E . YOUNG S MODULUS, LB/IN2

1 - AREA MOMENT OF HERTIA OF BEAM CROSS SECTION, INC 4 - LENGTH OF DEAM, IN 14 - MASS PER Unit LENGTH OF BEAM, LB-SSCIVM²

A + COEFFICIENT FROM TABLE BELOW

	NODES ARE INDICATED IN	TABLE BELOW AS A PE	TOPORTION OF LENGTH 1	MEASURED FROM LEFT	END
FIXED-FREE (CONTILEVED)	4 A11.52	4 0774 A+22.4	0 500 0 868	0 356 0644 0936	10 279 0 723 A + 200 0
HMGED-HINGED (SIMPLE)	4.507	0 500	0333 006;	0 25 050 075	020 040 060 080
FIXED-FIXED (BUILT-IN)	A-22.4	0 500	1 0259 0641	0270 0500 0772	1022710551
FREE-FREE	0224 0776 A . 22 4	0132 0500 0864	7 - 151 0 0 424 1 0 454 0 0 454	00.31 0.203 1 0.851 7 - 500	006-04-3 0773 0022710591 10940
FIXED - MINSEO	1	0562	1 0 544 0692 21 A 1104	1 0293 0780	102010415
HINGED - FREE	0.736	0446 0911 A 500	0309 0645 0844	- Sig Cab	0.4010381 10937

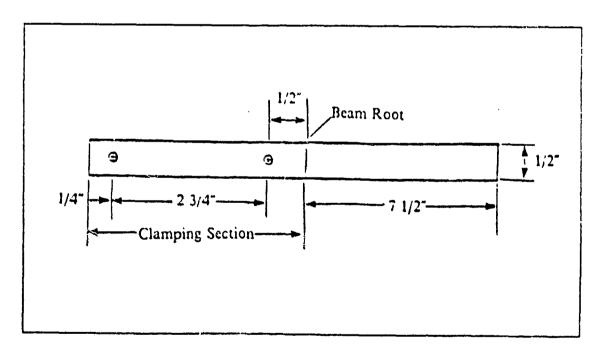


Figure B.1 Sonoston Beam Configuration

TABLE 2

CALCULATED RESONANT FREQUENCIES
OF CANTILEVER BEAMS

	Resonant Frequency (Hz)			
	Mode 1	Mode 2	Mode 3	
For the solution annealed beam:	20.6	131.4	361.9	
For the 1 hour aged beam:	21.9	139.4	384.0	
For the 2 hour aged beam:	24.9	158.6	436.9	

2. TORSION

Reference 8 also derives the natural frequency for torsional vibration. The equation for the natural frequency is:

$$\omega_{\mathbf{n}} = \sqrt{K_{\mathbf{r}}/(J_{\mathbf{o}} + 1/3J_{\mathbf{i}})}$$
 (B.2)

where:
$$K_r = G\pi d^4/321$$
 $J_1 = 2I_p\rho I_1$ $J_0 = \rho b/12(wl^3 + lw^3)$

For the samples tested:

length of the spherical section(l_1) = 12cm diameter of the spherical section(d) = 0.8cm length of the bottom section(l_2) = 12.0cm width of the bottom section(w) = 2.0cm height of the bottom section(b) = 2.5cm $I_p = \pi d^4/96$ $J_1 = 2(0.0201 \text{ cm}^4)(7.46 \text{ gm/cm}^3)12 \text{ cm} = 3.5998(\text{gm-cm}^2)$ $J_0 = 5520.4(\text{gm-cm}^2)$ G = E/(2(1+v)) where v = 0.3

The calculated natural frequencies for the torsion samples tested are listed in Table B.3.

TABLE 3

CALCULATED RESONANT FREQUENCIES

OF TORSION SAMPLES

	G	K _r	Resonant Frequency
	(Kg/cm ²)	(Kg-cm ²)	(Hz)
solution annealed sample:	0.473 x 10 ⁶	1585.0	84.5
I hour aged sample:	0.5325 x 10 ⁶	1784.0	89.6
2 hour aged sample:	0.6893 x 10 ⁶	2309.0	101.9

APPENDIX C

TORSION DAMPING APPARATUS DESIGN

In designing the torsion damping apparatus several requirements had to be met:

- 1. Minimizing extraneous energy loss (friction losses at the clamp interface, inherent loss in the clamp material, etc.).
- 2. Ensuring uniform stress distributions in the specimen.
- 3. Limiting the shaker to 25 pounds of force (before requiring forced air cooling).
- 4. The natural frequency of the specimen had to be less than 1000 hz.

The sample fits through the turning disc where it is held in place by 4 set screws (Figures C.1, C.2, and C.3) A bolt rests against the top of the specimen preventing it from moving vertically. The turning disc is supported by tapered roller bearings to prevent both radial and axial motion. The stand was designed to hold the turning disc and provide weight for stability (Figures C.4 and C.5). The shaker excites the apparatus by a "stinger" attached to the turning disc in the horizontal direction. Figure C.6 shows the assembled apparatus. The shaker also had a stand manufactured, elevating it to provide the horizontal input force (Figure C.7). Again, a heavy stand was made to ensure stability (eliminate any created moments). To meet the force requirements for the shaker the following equations were used to determine sample size:

Disc Mass =
$$\pi r^2 h \rho$$
 $I(DISC) = Mr^2/2$
a(disc acceleration) = $r\theta(2\pi f)^2$

$$F = Ia/r^2$$

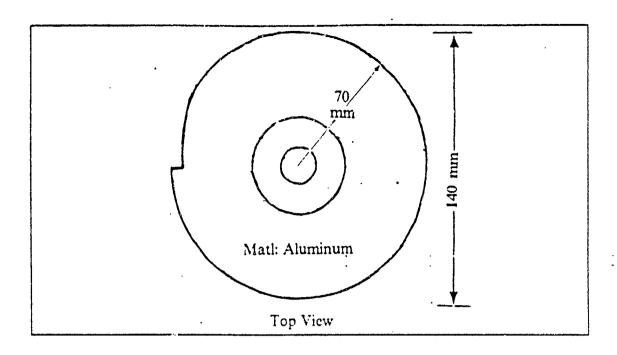


Figure C.2 Turning Disc - Top View

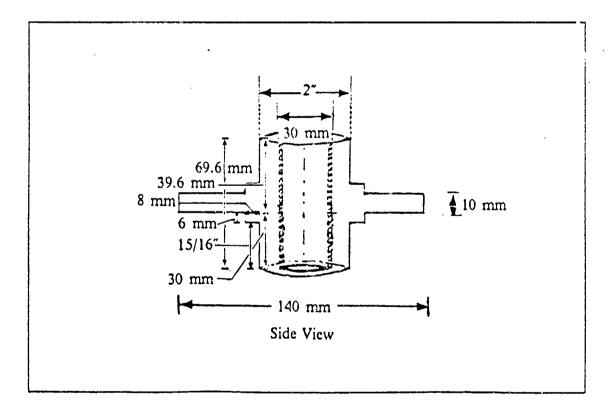


Figure C.3 Turning Disc - Side View

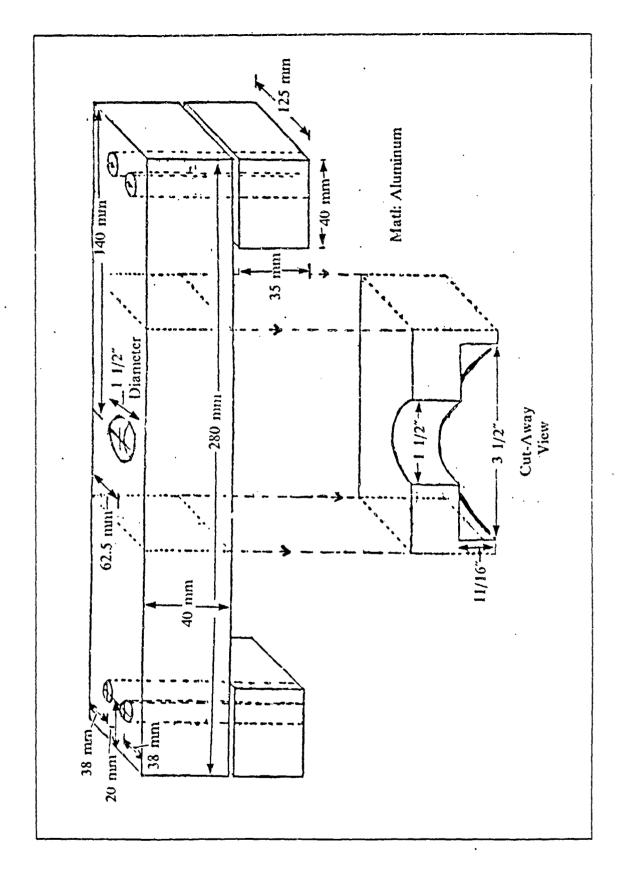


Figure C.4 Torsion Sample Upper Test Stand

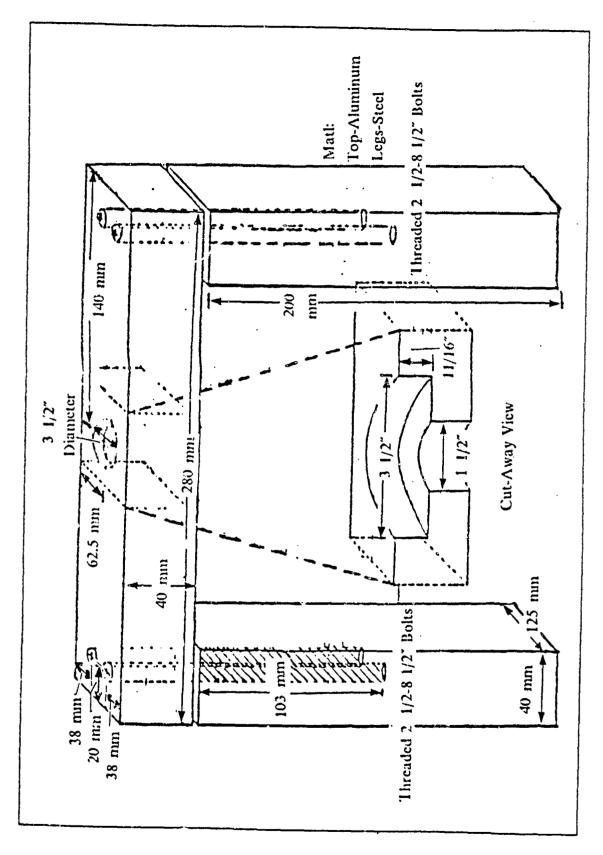


Figure C.5 Torsion Sample Lower Test Stand

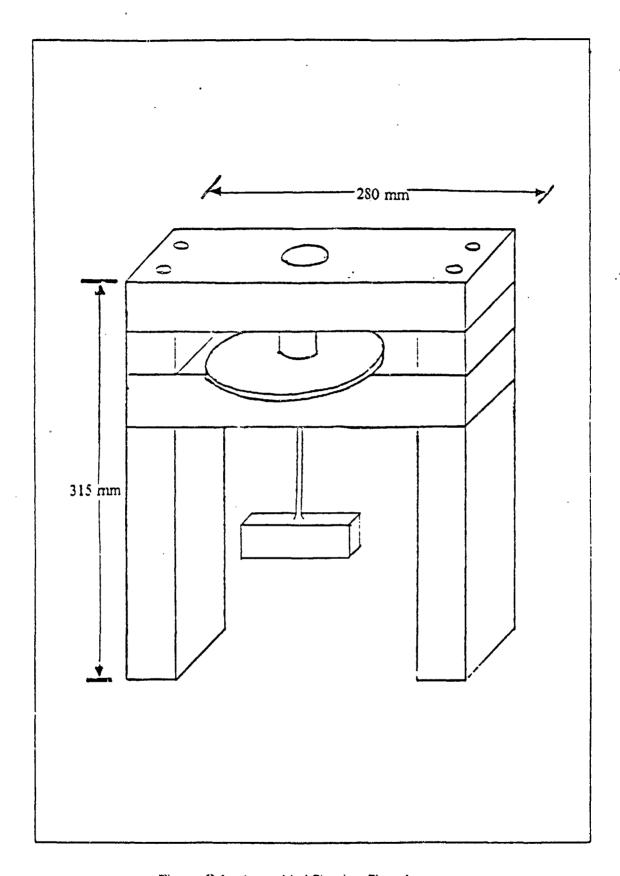


Figure C.6 Assembled Torsion Test Apparatus

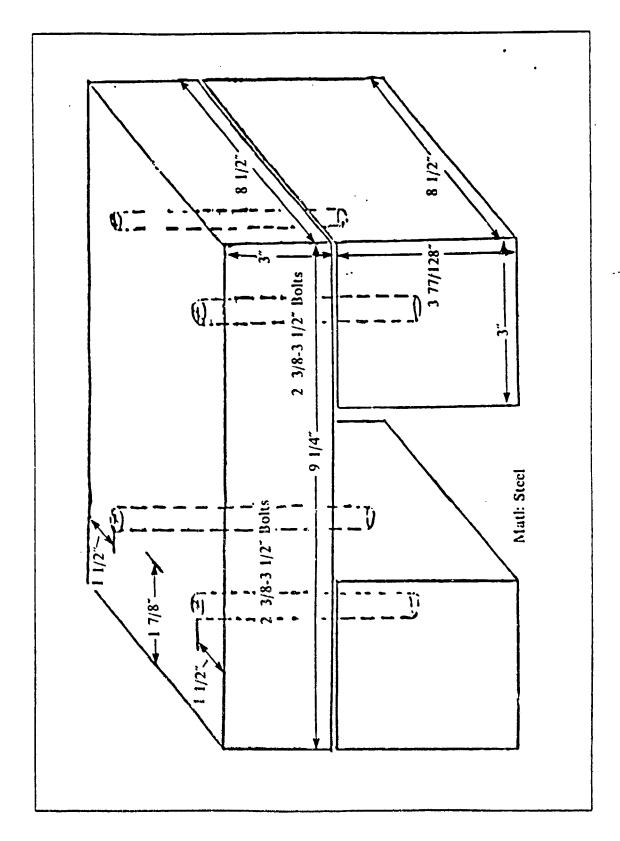


Figure C.7 Electromagnetic Shaker Stand for Torsion Test

APPENDIX D

CANTILEVER BEAM AND TORSION SAMPLE TRANSFER FUNCTION GRAPHS

1. CANTILEVER BEAM REPRESENTATIVE GRAPHS

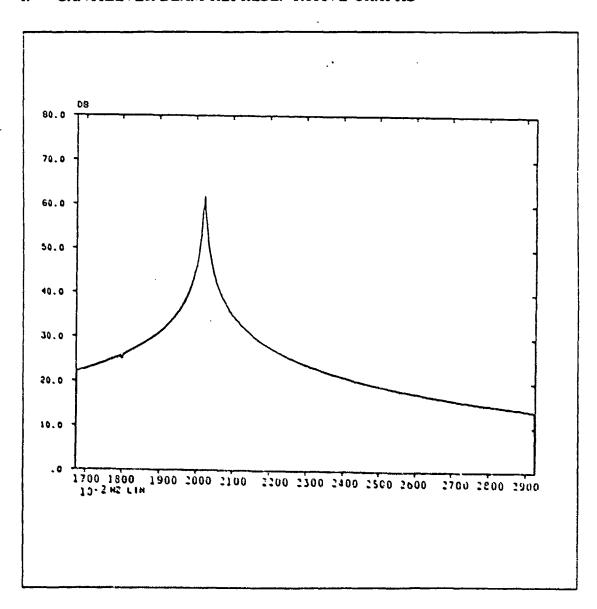


Figure D.1 Mode 1 - Solution Annealed Sample Transfer Function (Cantilever Beam - Random Input)

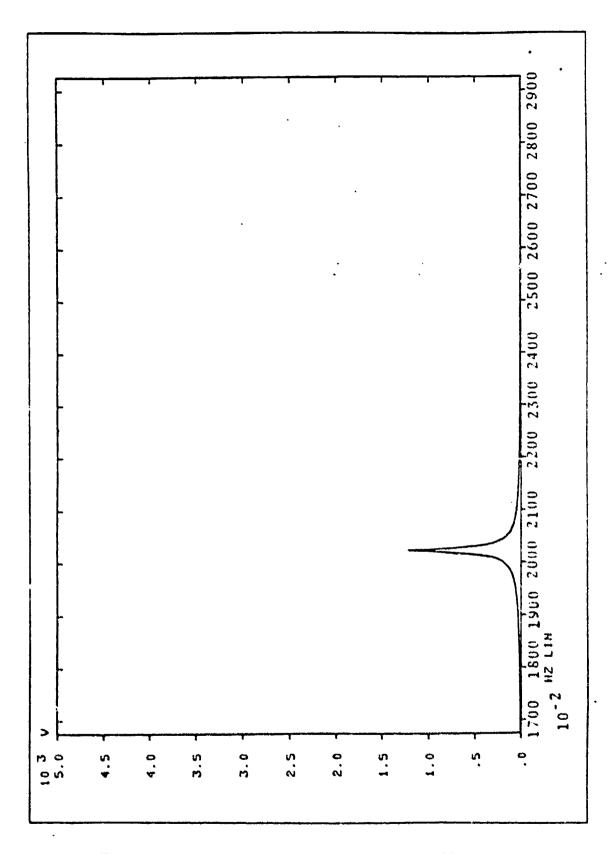


Figure D.2 Solution Annealed Transfer Function - Linear Scale (Cantilever Beam - Random Input)

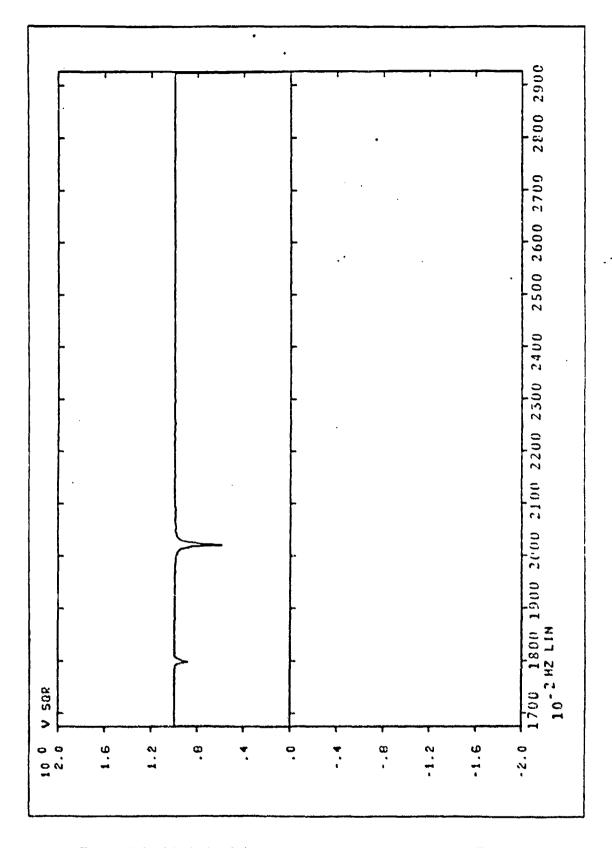


Figure D.3 Mode 1 - Solution Annealed Sample Coherence Function (Cantilever Beam - Random Input)

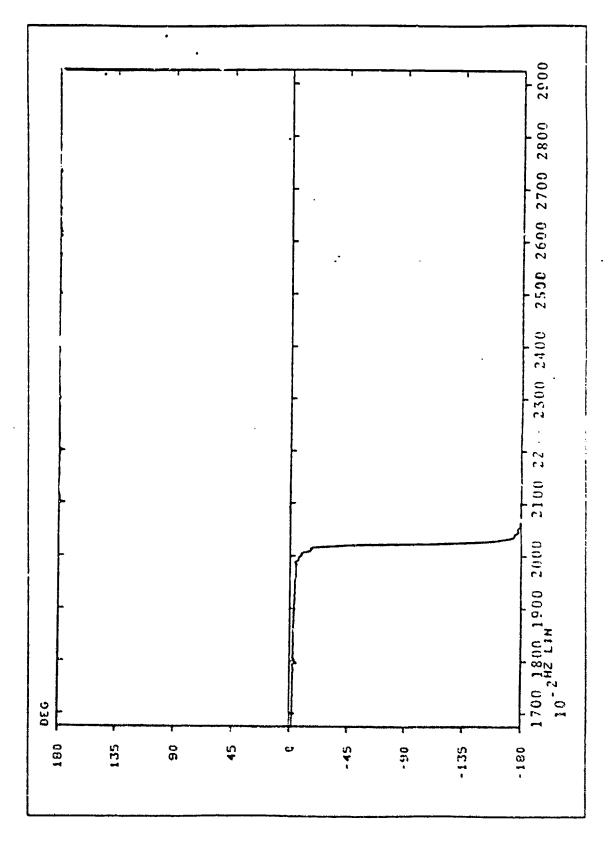


Figure D.4 Mode 1 - Phase Shift for the Solution Annealed Sample (Cantilever Beam - Random Input)

2. TORSION SAMPLE REPRESENTATIVE GRAPHS

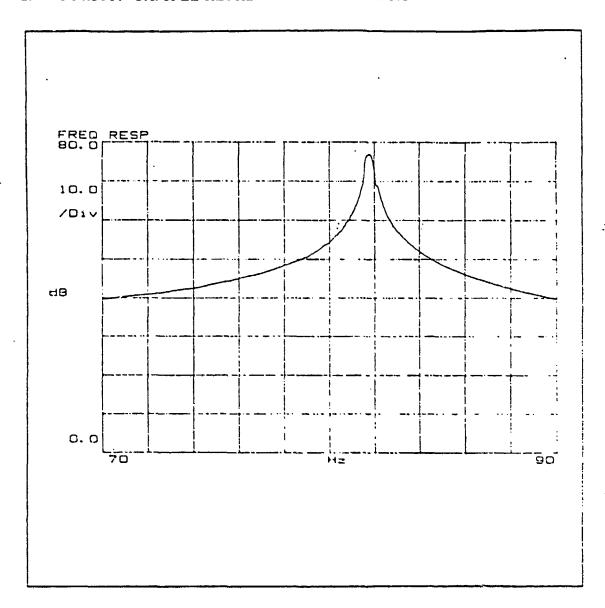


Figure D.5 Solution Annealed Transfer Function (Torsion Sample - Random Input)

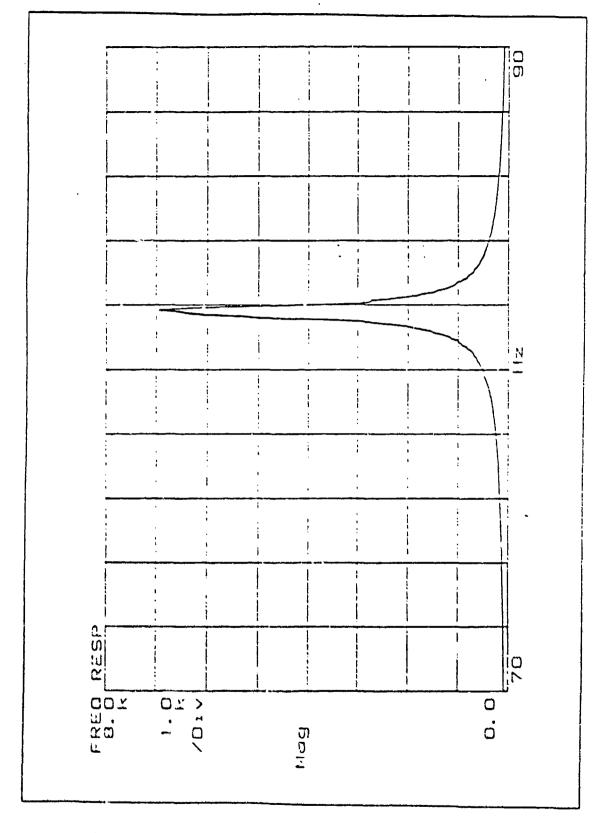


Figure D.6 Solution Annealed Transfer Function - Linear Scale (TorsionSample - Random Input)

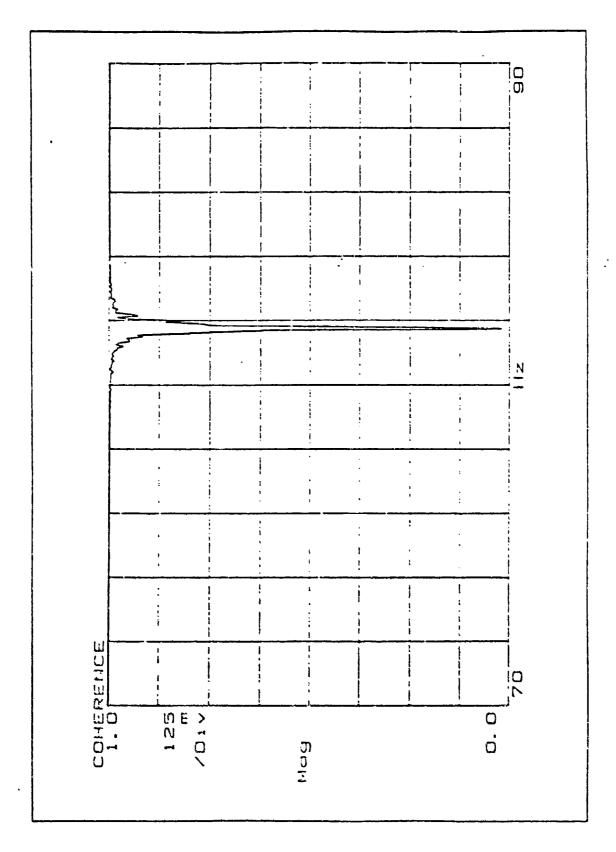


Figure D.7 Solution Annealed Sample Coherence Function (Torsion Sample - Random Input)

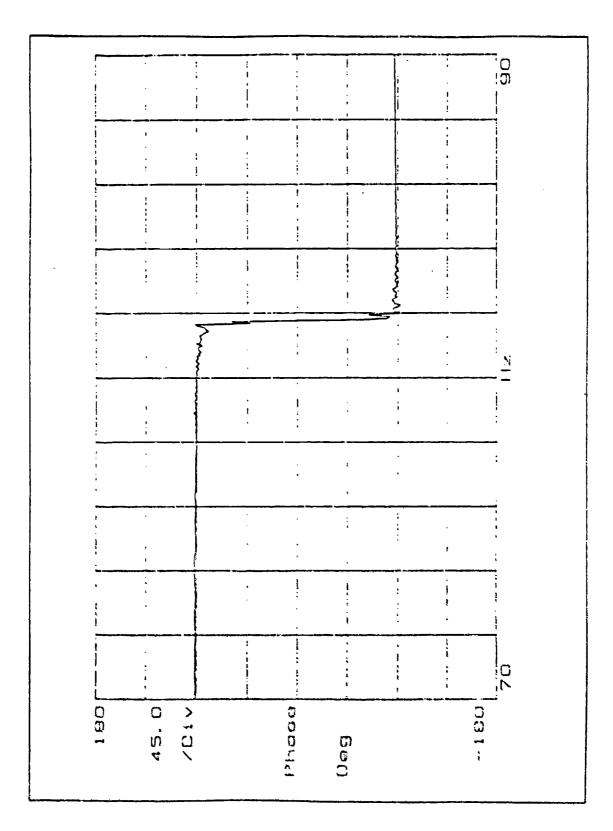


Figure D.S Torsion - Phase Shift for Solution Annealed Sample (Torsion Sample - Random Input)

APPENDIX E CANTILEVER BEAM AND TORSION SAMPLE DATA

1. CANTILEVER BEAM DATA

TABLE 4
MODE 1 - AS QUENCHED SAMPLE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
20.275 20.2909 20.2476 20.242 20.242 20.237 20.2176 20.237 20.162 20.168 20.1443	.336 .3288 .329 .337 .429 .4631 .4722 .5308 .5514 .55102	.0123 .0123 .0146 .0146 .0167 .0167 .0202 .02152 .02152 .0225	.4978 .4978 .5809 .5809 .6046 .6041 .743 .743 .8179 .8179 .8853	20.2409 20.2575 20.2143 20.2079 20.1986 20.1901 20.1732 20.1895 20.1168 20.0888 20.0986	20.3091 20.3245 20.2809 20.2761 20.2854 20.2859 20.2620 20.2848 20.2152 20.2192 20.1998 20.2014

TABLE 5 MODE 1 - 1 HOUR AGED SAMPLES

MODE 1						
FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	Fl (HZ)	F2 (HZ)	
		SAMPLE	\$ 1			
21.8800 21.8846 21.8635 21.8656 21.8474 21.7456 21.7527 21.7274 21.7315 21.7656 21.6512 21.6511 21.5445 21.5445	1.54 1.38 1.60 1.58 1.69 1.61 1.77 2.76 1.77 2.76 1.62 1.68 1.99	.01436 .01436 .01436 .01564 .01564 .01801 .01801 .01987 .01987 .01987 .01987 .02099 .02099	0.5160 0.5160 0.5160 0.5790 0.5790 0.6334 0.6334 0.7439 0.7439 0.7439 0.8041 0.8041 1.0524	21.7115 21.7339 21.6881 21.6932 21.6628 21.5705 21.5968 21.55351 21.5351 21.5744 21.4809 21.4777 21.4762 21.3635 21.3303	22.0485 22.0353 22.0389 22.0320 21.9207 21.8904 21.9384 21.9509 21.9568 21.8215 21.8215 21.8260 21.7255 21.7587	
		SAMPLE	12			
21.8629 21.8740 21.8482 21.7527 21.7537 21.7191 21.7315 21.6537 21.5489 21.5545	1.56 1.56 1.59 1.71 1.71 1.76 1.80 1.82 1.79 1.89	.0145 .0145 .01573 .01573— .018 .018 .01986 .01986 .02099 .02099	.5 .5819 .5819 .637 .637 .7429 .7429 .806 .806 1.04	21.6924 21.7034 21.6743 21.6721 21.5670 21.5655 21.5283 21.5359 21.4671 21.4599 21.3347 21.3508	22.0334 22.0446 22.0221 22.0217 21.9384 21.9419 21.9099 21.9271 21.8605 21.8475 21.7582	

TABLE 6 MODE 1 - 2 HOUR AGED SAMPLES

INPUT ACCEL (G)	FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	F1 (HZ)	F2 (HZ)
		SAMPLE	‡ 3		
.5637 .5637 .5888 .5888 .5998 .6535 .6535 .7503 .7503 .8025	24.9000 24.8700 24.7400 24.7330 24.5600 24.5951 24.6800 24.6750 24.4011 24.5200 24.0350 24.1000	2.6605 2.7895 3.0397 3.0618 3.0496 2.9581 3.1223 3.277 3.32411 4.6176 4.5783	.00407 .00407 .00732 .00732 .008296 .01104 .01104 .01317 .01317	24.5687 24.5231 24.3640 24.3499 24.1840 24.2201 24.3150 24.2898 24.0013 24.1125 23.4801 23.5483	25.2312 25.2169 25.1160 25.1160 24.9360 24.9701 25.0450 25.0602 24.8009 24.9275 24.5899 24.6517
		SAMPLE	84		
.4554 .4554 .5611 .5611 .5895 .5895 .6732 .6732 .7502 .8086 .8086	25.1600 25.1396 25.0252 25.0000 24.6818 24.6800 24.5674 24.5200 24.4148 24.4400 24.0714 24.0400	2.4698 2.2733 2.8773 2.8084 2.9718 3.0733 2.8898 3.1648 3.3048 3.2381 4.3338 4.59059	.004099 .004099 .007375 .007375 .00838 .00838 .01085 .01085 .01306 .01306	24.8493 24.8538 24.6651 24.6489 24.3150 24.3007 24.2125 24.1320 24.0113 24.0443 23.5498 23.4882	25.4707 25.4253 25.3852 25.3510 25.0592 24.9224 24.9080 24.8182 24.8357 24.5930 24.5918

TABLE 7 MODE 2 - AS QUENCHED SAMPLE

AS QUENCHED SAMPLE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	Fl (HZ)	F2 (HZ)
130.65 130.539 130.587 130.539 130.48 130.478 130.338 130.413 130.386 130.347	.3476 6 .3312 .4982 5 .4001 .3833 .3646 .3297	.00587 .00587 .00831 .00831 .01579 .01579 .02143 .02143 .02843 .02843	.5749 .5749 .6438 .6438 .8068 .9419 .9419 1.336 1.775	130.4370 130.3869 130.3600 130.3234 130.1869 130.2500 130.2250 130.1980 130.1449 130.2000 130.2344	130.8000 130.7837 130.8139 130.7557 130.7800 130.7090 130.7006 130.6280 130.6396 130.6396 130.6564

TABLE 8 MODE 2 - 1 HOUR AGED SAMPLES

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
		SAMPL	E #1		
138.6977 138.2788 139.6987 139.8792 142.6800 142.5700 143.0200 143.0400 144.0000 144.0700 144.1300	2.7278 2.7500 2.1672 1.9806 1.7833 1.8637 1.1086 0.8816 0.8811 0.8430 0.2710 0.2853	0.02614 0.02614 0.02600 0.02000 0.01625 0.01625 0.01410 0.01410 0.00995 0.00995	1.2949 1.2949 0.8612 0.8612 0.8059 0.7252 0.7252 0.6008 0.5181 0.5181	136.8060 136.3775 138.1849 138.4939 141.2415 142.2272 142.4095 141.4718 143.3930 143.8748 143.9244	140.5894 140.1801 141.2125 141.2644 143.9522 143.8985 143.8705 143.2282 144.6064 144.2652 144.3356
		SAMPL	E #2		
144.1100 144.0800 144.1000 143.8000 143.0100 143.0140 142.6400 142.5900 139.6982 139.7006 138.4352 138.5217	0.2730 0.2750 0.8560 0.8732 0.8875 0.8984 1.7943 1.8217 1.9432 2.0321 2.7184 2.7337	0.0064 0.0064 0.00989 0.00989 0.01450 0.01450 0.01632 0.01632 0.02250 0.02250 0.02250	0.5184 0.5184 0.6021 0.6021 0.7227 0.7227 0.8066 0.8066 0.8620 1.2391	143.9133 143.8819 143.4833 143.1722 142.3754 142.3716 141.3603 141.2912 138.3409 138.2812 136.5536 136.6283	144.3067 144.2781 144.7167 144.4278 143.6446 143.6564 143.8888 141.0555 141.1200 140.3168 140.4151

TABLE 9 MODE 2 - 2 HOUR AGED SAMPLES

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (%)	F1 (HZ)	F2 (HZ)
		SAME	PLE #3		
159.4200 159.4600 159.1600 159.1800 158.6800 158.7200 158.6100 158.6000 158.2600 158.2000 157.8300 157.6800	1.0780 1.0600 1.1815 1.1865 1.2690 1.2740 1.3311 1.3657 1.4239 1.3607 1.8664 1.8273	.0044 .0044 .0067 .0067 .0085 .0085 .0088 .0116 .0116	.5221 .5221 .6008 .6008 .6510 .7192 .7192 .8094 .8094 1.1575	158.5608 158.2197 158.2356 157.6732 157.7089 157.5543 157.5169 157.1332 157.1237 156.3572	160.2793 160.3051 160.1002 160.1243 159.6868 159.7310 159.6656 159.6830 159.3867 159.2763 159.3029 159.1206
		SAMI	PLE #4		
159.4837 159.4794 159.1600 159.1437 158.7600 158.7265 158.5200 158.5048 158.2000 158.1750 157.8000	1.0346 1.0500 1.1889 1.1894 0.9700 1.2114 1.1134 1.0978 1.4587 1.3427 2.0025 1.8745	.0042 .0042 .0067 .0067 .0084 .0097 .0097 .0115 .0115	.4606 .4606 .6005 .6073 .6473 .7190 .7190 .8067 .8067 1.1538	158.6587 158.6422 158.2137 158.1972 157.9899 157.7651 157.6375 157.6347 157.0461 157.1131 156.2199 156.3409	160.3087 160.3167 160.1060 160.0901 159.5299 159.6879 159.3748 159.3538 159.3538 159.2369 159.3799

TABLE 10 MODE 3 - AS QUENCHED SAMPLE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	FZ (HZ)
361.8380 361.8370 361.2750 361.2371 361.1750 361.0130 361.0540 361.0130 361.0235 360.912	.2109 .1858 .2192 .3041 .263 .2955 .3357 .3381 .426 .4227	.0025 .0025 .0027 .0027 .0031 .0031 .0039 .0045 .0045	.4997 .4997 .6034 .6034 .6846 .7322 .7322 .8793 .8793 1.1274	361.3750 361.4500 360.8380 360.8099 360.6567 360.4750 360.4131 360.2220 360.2605 360.1540 360.1383	362.1380 362.1223 361.6380 361.9086 361.6000 361.6339 361.6339 361.7500 361.7500 361.7500 361.665

TABLE 11 MODE 3 - 1 HOUR AGED SAMPLES

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
		SAMI	PLE #1	.•	
384.6400 384.6286 383.4921 383.4800 382.5002 382.6000 382.0427 381.9200 381.5849 381.4400 381.4704 381.2800	1.0294 1.1075 1.2459 1.3038 1.2092 1.2337 1.2632 1.3091 1.1797 1.1745 1.3993	.0016 .0016 .0019 .0019 .0026 .0026 .0034 .0035 .0035	.5815 .5815 .6373 .6373 .6934 .7436 .7436 .8975 .8975 1.1833	382.6603 382.4987 381.1031 380.9801 380.1876 380.2399 379.6297 379.4201 379.3341 379.1999 378.8014 378.5226	386.6197 386.7585 385.8811 385.9799 384.8128 384.9601 384.4557 384.4199 383.8357 383.6800 384.1394 384.0374
		SAME	PLE #2		
384.6052 384.6327 383.4917 383.4852 382.5132 382.5894 382.6427 382.0952 381,5721 381.4982 381.3527 381.4407	1.0524 1.1905 1.2743 1.3009 1.2143 1.2247 1.2821 1.3020 1.1800 1.1762 1.4020 1.4243	.0016 .0016 .0020 .0027 .0027 .0034 .0036 .0036	.5892 .5892 .6451 .7029 .7029 .7444 .9001 .9001 1.1578	382.5814 382.5163 381.0483 380.9908 380.1908 380.2466 380.1898 379.6078 379.3208 379.3208 379.2546 378.6794 378.7243	386.6289 386.7491 385.9351 385.9796 384.8356— 384.9322 385.0956 384.5826 383.8234 383.7418 384.0259 384.1571

TABLE 12 MODE 3 - 2 HOUR AGED SAMPLES

FN (HZ) (G)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
		SAMP	LE #3		
444.9035 444.9600 444.7191 444.7200 444.66498 444.6800 444.2365 444.2365 444.2365 444.2365 444.2365 444.2365 444.2365 444.2365 444.2365	1.5876 1.6000 1.7136 1.7612 1.7080 1.8463 1.8789 1.8484 1.9779 2.0117 2.1801 2.1709	.00248 .00266 .00266 .00304 .00306 .00306 .00451 .00451 .00588	.4343 .4343 .4754 .6754 .6830 .7312 .7312 .8867 .8867	441.3719 441.4003 440.9087 440.8525 440.8525 440.5749 440.0631 440.1541 439.3912 439.2159 438.3935 438.3102	448.4351 448.5197 448.5295 448.6362 448.4471 448.7851 448.4099 448.3659 448.1688 448.1414 448.0563 447.9298
		SAMP	LE #4		
444.2800 444.2600 444.2000 444.2467 443.9553 444.9500 443.9600 443.9600 443.8400 443.8784 443.1600 443.1500	1.6362 1.6132 1.7929 1.7868 1.8376 1.8154 1.8780 1.8488 2.0128 2.0191 2.1866 2.2051	.00261 .00261 .00278 .00278 .00310 .00310 .00313 .00400 .00400 .00613	.4676 .4676 .4797 .4797 .7027 .7027 .7379 .8686 .8686 1.2920	440.6453 440.6766 440.2179 440.2778 439.8762 440.0094 439.7912 439.8133 439.3732 439.3732 439.3972 438.3149 438.2640	447.9147 447.8434 448.1820 448.0344 448.0706 448.1288 448.0205 448.3068 448.3596 448.0051 448.0359

TABLE 13 MODE 1 - UNAGED SAMPLE (SWEPT SINE)

MODE 1 SWEPT SINE TEST

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
20.2750 20.2750 20.2590 20.2570 20.2450 20.1750	.3951 .3951 .4136 .6447 .5947 .7891	.0123 .0146 .0167 .0215 .0225	.5529 .5558 .5599 .5675 .5757	20.2349 20.2349 20.2171 20.1917 20.1848 20.0954	20.3150 20.3150 20.3009 20.3223 20.3052 20.2546

TABLE 14

MODE 1 - 1 HOUR AGED SAMPLES (SWEPT SINE)

MODE 1 SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
	-	-SAMP	LE #1		
21,8600 21.8200 21.7200 21.7000 21.6800 21.6500 21.5400	1.4904 1.5399 1.6400 1.7005 1.6799 1.8199	.01530 .01484 .01583 .01792 .01964 .02101	0.5204 0.5316 0.5822 0.6287 0.7269 0.7943 1.0109	21.6971 21.6520 21.5419 21.5155 21.4979 21.4530 21.3257	22.0229 21.9880 21.8981 21.8845 21.8621 21.8470 21.7543
		SAMP	LE #2		
21.8600 21.8400 21.7500 21.7100 21.6600 21.5400 21.4900	1.5297 1.5897 1.7205 1.7402 1.7996 1.9601 1.8799	.01463 .01602 .01834 .01977 .02084 .02321	0.5204 0.5795 0.6298 0.7431 0.8019 1.1000	21.6928 21.6664 21.5629 21.5211 21.4651 21.3289 21.2880	22.0272 22.0136 21.9371 21.8989 21.8549 21.7511 21.6920

TABLE 15 MODE 1 - 2 HOUR AGED SAMPLES (SWEPT SINE)

2 HOUR AGED SAMPLES

MODE 1 SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	STRAIN (2)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ) .	
		SAM	PLE #3			
25.010 24.98 24.96 24.58 24.54 26.51 24.27	1.8760 1.9055 2.9223 3.0016 3.0391 3.2060 3.8475	.0023 .0033 .0071 .0097 .0120 .0123	.4851 .5333 .5819 .6305 .6789 .7270	24.7754 24.7420 24.5953 24.2111 24.1621 24.1171 23.8031	25.2446 25.2180 25.3247 24.9489 24.9079 24.9029 24.7369	
SAMPLE #4						
25.013 24.992 24.927 24.571 24.543 24.498 24.301	1.8806 1.9094 2.8989 3.0125 3.0289 3.2141 3.8624	.0023 .0031 .0048 .0099 .0128 .0126	.4912 .5298 .5752 .6317 .6804 .7275	24.7778 24.7534 24.5657 24.2009 24.1713 24.1043 23.8317	25.2482 25.2306 25.2883 24.9411 24.9147 24.8917 24.7703	

TABLE 16

MODE 2 - UNAGED SAMPLE (SWEPT SINE)

AS QUENCHED SAMPLE

MODE 2 SWEPT SINE TEST

FN (HZ)	LOSS FACTOR (%)	STRAIN (2)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
130.6500	.3253	.0053	.5503	130.4375	130.8625
130.4250	.3734	.0057	.5615	130.1815	130.6685
130.3750	.3835	.0060	.5835	130.1250	130.6250
130.3500	.4218	.0105	.6132	130.0751	130.6249
130.3750	.4349	.0115	.6201	130.0915	130.6585
130.4500	.4638	.0124	.6521	130.1475	130.7525

TABLE 17 MODE 2 - 1 HOUR SAMPLES (SWEPT SINE)

1 HOUR HEAT TREATED SAMPLES

MODE 2 SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)	
		SAMPL	E #1			
138.1487 140.8892 142.4606 142.9968 144.0149 144.1266	2.8100 2.1006 1.8427 1.1820 0.8430 0.3253	.03104 .02064 .01584 .01488 .01095	1.3109 0.9012 0.8259 0.7189 0.6143 0.5421	136.2077 139.4095 141.1480 142.1517 143.4079 143.8922	140.0897 142.3689 143.7732 143.8419 144.6219 144.3610	
SAMPLE #2						
144.0080 144.1250 143.1980 142.6100 140.0841 138.5522	0.2854 0.8723 0.8984 1.7793 2.0145 2.7069	.0039 .01205 .01534 .01721 .02540	0.5873 0.6117 0.7341 0.7998 0.8451 1.2895	143.8025 143.4964 142.5548 141.3413 138.6731 136.6769	144.2135 144.7536 143.8412 143.8787 141.4951 140.4274	

TABLE 18

MODE 2 - 2 HOUR SAMPLES (SWEPT SINE)

2 HOUR AGED SAMPLES

MODE 2 SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (8Z)	F2 (HZ)
		SAM	PLE #3		
159.730 159.380 159.210 158.960 158.670 156.590 158.340	0.9103 1.1068 1.1406 1.2217 1.3008 1.3652	.0031 .0048 .0059 .0071 .0086 .0089	.4851 .5333 .5819 .6305 .6789 .7274 .7759	159.0030 158.4980 158.3020 157.9890 157.6380 157.5075 157.2243	160.4570 160.2620 160.1150 159.9310 159.7020 159.6725 159.4557
		SAM	PLE 14		
159.690 159.350 159.240 153.930 158.580 158.520 158.360	0.9115 1.1099 1.1601 1.2207 1.3026 1.3984	.0033 .0050 .0050 .0060 .0072 .0086 .0090	.4902 .5365 .5824 .6334 .6821 .7301	158.9628 158.4657 158.3163 157.9600 157.5472 157.4116 157.2421	160.4178 160.2343 160.1637 159.9000 159.6128 159.6284 159.4779

TABLE 19 MODE 3 - UNAGED SAMPLE (SWEPT SINE)

MODE 3 SWEPT SINE TEST

FN (HZ)	LOSS FACTOR (%)	STRAIN (%).	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
361.8000 361.3750 361.1000 360.8000 360.7500	.1899 .2119 .2875 .3983 .3900	.00113 .00141 .00209 .00273	.4560 .4899 .6099 .6799 .7820	361.4563 360.9921 360.5809 360.0815 360.0465	362.1437 361.7579 361.6191 361.5185 361.4535

TABLE 20
MODE 3 - 1 HOUR AGED SAMPLES (SWEPT SINE)

M	מס	E	3		
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		One:	· · · · · ·		
FN (HZ)	LOSS FACTOR (%)	STRAIN (X)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
		SAMPLE	E 01		
384.620 283.420 382.640 381.880 381.560 381.200	1.2155 1.2868 1.2569 1.3121 1.3214 1.4541	.0020 .0024 .0029 .0033 .0037	.6015 .6279 .7015 .7581 .9032 1.1698	382.2825 380.9531 380.2353 379.3747 378.8404 378.4285	336.9575 385.8869 385.0447 384.3853 383.8796 383.9715
		SAMPLE	E #2		
384.640 383.540 382.860 382.360 381.860 331.240	1.1876 1.2074 1.2208 1.2786 1.3284 1.4021	.0018 .0024 .0028 .0036 .0037 .0040	.5882 .6190 .7002 .7641 .9011	382.3560 51.2246 380.5230 379.9156 379.3237 378.5673	386.9240 335.8554 385.1970 364.8044 384.3963 383.9127

TABLE 21 MODE 3 - 2 HOUR SAMPLES (SWEPT SINE)

			ODE 3 PT SINE		
FN (HZ)	LOSS FACTOR (%)	STRAIN (%)	INPUT ACCEL (G)	F1 (HZ)	F2 (HZ)
		SAM	PLE #3		
444.7091 444.7137 444.6998 444.6947 444.6902 444.3011 444.3007	1.7831 1.7812 1.7907 1.8395 1.8575	.00266 .00261 .00269 .00286 .00299 .00300	.4851 .5333 .5819 .6305 .6789 .7274 .7759	440.8086 440.7489 440.7393 440.7131 440.6002 440.1747 440.0881	448.6785 448.6785 448.6603 448.6763 448.7802 448.4275 448.5133
		SAM	PLE #4		
444.7184 444.7102 444.6681 444.6754 444.6732 444.3241	1.8131 1.8324 1.8136 1.8582 1.8664	.00271 .00284 .00285 .00292 .00325 .00318	.4902 .5284 .5823 .6312 .6777 .7301	440.7599 440.6787 440.5941 440.6431 440.5417 440.1777	448.6768 448.7417 448.7421 448.7077 448.8047 448.4705 448.5635

2. TORSION SAMPLE DATA

TABLE 22
TORSION - SOLUTION ANNEALED SAMPLE (RANDOM INPUT)

St	DLUTION ANN	EALED SAM	PLE
FN	LOSS	INPUT	STRAIN
(HZ)	FACTOR	ACCEL	(%)
	(%)	(G)	
83.32	.1776	.5846	.002045
83.28	.2282	.5992	.002439
83.18	.2741	.6022	.002564
83.12	.3008	.6292	.002911
83.12	.3200	.6355	.002958
82.84	.3283	.6458	.003539
82.5	.3345	.6505	.003655
82.19	.3601	.6564	.003986
81.56	.3654	.6621	.004577

TABLE 23
TORSION - SOLUTION ANNEALED SAMPLE (SWEPT SINE)

SOLUTION ANNEALED SAMPLE

SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	INPUT ACCEL (G)	STRAIN (%)
83.20 81.85 81.70 81.35 80.95 80.823	.2860 .3665 .3917 .4376 .4917 .5419	.6104 .6210 .6826 .7362 .7553 .7659	.002445 .004611 .005393 .007064 .009055

TABLE 24
TORSION - 1 HOUR AGED SAMPLE (RANDOM INPUT)

1 HOUR AGED SAMPLE

FN (HZ)	LOSS FACTOR (%)	INPUT ACCEL (G)	STRAIN (%)
68.875 68.775 68.750 68.650 68.525 68.400 68.300 68.375 67.650	1.1397 1.1458 1.1549 1.2207 1.6417 1.7544 2.2577 3.0903	.5711 .5810 .6007 .6279 .6353 .6463 .6512 .6554	.001505 .002552 .002553 .003593 .003805 .004459 .004723 .004653

TABLE 25 TORSION - 1 HOUR AGED SAMPLE (SWEPT SINE)

1 HOUR AGED SAMPLE

SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	INPUT ACCEL (G)	STRAIN (%)
68.400 68.075 68.075 67.725 67.700 67.475 67.325 67.125 66.925	1.6812 1.9464 2.0566 2.3256 2.6209 2.9306 3.2107 3.6305 3.9137	.5739 .5735 .6015 .6247 .6353 .6459 .6509	.003224 .003488 .004333 .005904 .007004 .007213 .008068 .008889

TABLE 26 TORSION - 2 HOUR AGED SAMPLE (RANDOM INPUT)

2 HOUR AGED SAMPLE

FN (HZ)	LOSS FACTOR (%)	INPUT ACCEL (G)	STRAIN (%)
68.346	1.5714	.5923	.004135
68.100	2.1806	.6764	.008949
67.844	2.8339	.7044	.010144
67.400	3.1899	.7351	.013658
67.375	3.4137	.7489	.018575
67.375	3.6735	.7639	.020472

TABLE 27 TORSION - 2 HOUR AGED SAMPLE (SWEPT SINE)

2 HOUR AGED SAMPLE

SWEPT SINE

FN (HZ)	LOSS FACTOR (%)	INPUT ACCEL (%)	STRAIN (%)
68.875 68.175 67.875 67.450 67.250	1.1252 1.4668 2.8405 4.0030 4.0537 4.1290	.6176 .6236 .6973 .7214 .7509	.005121 .008149 .010497 .014514 .018386

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